

Network Working Group
Internet-Draft
Intended status: Informational
Expires: December 5, 2016

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June 3, 2016

The Security Evaluated Standardized Password Authenticated Key Exchange
(SESPAKE) Protocol
draft-smyshlyayev-sespake-05

Abstract

This document specifies the Security Evaluated Standardized Password Authenticated Key Exchange (SESPAKE) protocol. The SESPAGE protocol provides password authenticated key exchange for usage in the systems for protection of sensitive information. The security proofs of the protocol was made for the case of an active adversary in the channel, including MitM attacks and attacks based on the impersonation of one of the subjects.

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1. Introduction

The current document contains the description of the password authenticated key exchange protocol SESPKE (security evaluated standardized password authenticated key exchange) for usage in the systems for protection of sensitive information. The protocol is intended to use for establishment of keys that are then used for organization of secure channel for protection of sensitive information. The security proofs of the protocol was made for the case of an active adversary in the channel, including MitM attacks and attacks based on the impersonation of one of the subjects.

2. Conventions used in this document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC2119].

3. Notations

This document uses the following parameters of elliptic curves in accordance with [RFC6090].

E an elliptic curve defined over a finite prime field GF(p), where $p > 3$;

p the characteristic of the underlying prime field;

a, b the coefficients of the equation of the elliptic curve in the canonical form;

m the elliptic curve group order;

q the elliptic curve subgroup order;

P generator of the subgroup of order q;

X, Y the coordinates of the elliptic curve point in the canonical form;

O zero point (point of infinity) of the elliptic curve.

This memo uses the following functions:

HASH the underlying hash function;

HMAC the function for calculating a message authentication code, based on a HASH function in accordance with [RFC2104];

F(PW, salt, n) the value of the function PBKDF2(PW,salt,n,len), where PBKDF2(PW,salt,n,len) is calculated according to [RFC2898] The parameter len is considered equal to minimal integer that is a multiple of 8 and satisfies the following condition:
 $\text{len} \geq \text{floor}(\log_2(q))$.

This document uses the following terms and definitions for the sets and operations on the elements of these sets

B_n the set of byte strings of size n, $n \geq 0$, for $n = 0$ the B_n set consists of a single empty string of size 0; if b is an element of B_n, then $b = (b_1, \dots, b_n)$, where b_1, \dots, b_n are elements of $\{0, \dots, 255\}$;

int(w') if the byte string $w' = (w_1, \dots, w_t)$ is in B_t, then $\text{int}(w')$ is an integer $w = 256^{(t-1)}w_t + \dots + 256^{(0)}w_1$;

INT(w') if the byte string $w' = (w_1, \dots, w_t)$ is in B_t, then $\text{INT}(w')$ is an integer $W = 256^{(t-1)}w_1 + \dots + 256^{(0)}w_t$;

|| concatenation of byte strings A and C, i.e., if A in B_n1, C in B_n2, A = (a_1,a_2,...,a_n1) and C = (c_1,c_2,...,c_n2), then A||C = (a_1,a_2,...,a_n1,c_1,c_2,...,c_n2) is an element of B_(n1+n2);

Byte representation of a point (X,Y). If (X, Y) is an elliptic curve point then the byte representation of (X,Y) is a concatenation of the coordinates of this point X||Y; the length of the byte representations of the coordinates X and Y is equal to the minimum possible length of the byte representation of the subgroup generator p.

4. Mathematical definitions

Suppose a prime number $p > 3$ is given. Then, an elliptic curve E, defined over a finite prime field $GF(p)$, is the set of number pairs (x,y) , where x and y belong to F_p , satisfying the identity:

$$y^2 = x^3 + a * x + b \pmod{p},$$

where a, b belong to $GF(p)$ and $4 * a^3 + 27 * b^2$ is not congruent to zero modulo p.

An invariant of the elliptic curve is the value $J(E)$, satisfying the equality:

$$J(E) = \frac{4 * a^3}{4 * a^3 + 27 * b^2} \pmod{p},$$

Elliptic curve E coefficients a, b are defined in the following way using the invariant $J(E)$:

$$\begin{cases} a = 3 * k \pmod{p}, \\ b = 2 * k \pmod{p}, \end{cases}$$

$$J(E) \text{ where } k = \frac{J(E)}{1728 - J(E)} \pmod{p}, \quad J(E) \neq 0 \text{ or } 1728.$$

The pairs (x, y) satisfying the identity (1) are called "the elliptic curve E points"; x and y are called x- and y-coordinates of the point, correspondingly.

We will denote elliptic curve points as $Q(x, y)$ or just Q. Two elliptic curve points are equal if their x- and y-coordinates are equal.

On the set of all elliptic curve E points, we will define the addition operation, denoted by "+". For two arbitrary elliptic curve E points Q1 (x_1, y_1) and Q2 (x_2, y_2), we will consider several variants.

Suppose coordinates of points Q1 and Q2 satisfy the condition $x_1 \neq x_2$. In this case, their sum is defined as a point Q3 (x_3, y_3), with coordinates defined by congruencies:

$$\begin{aligned} | & x_3 = \lambda^2 - x_1 - x_2 \pmod{p}, \\ | & y_3 = \lambda * (x_1 - x_3) - y_1 \pmod{p}, \\ & \text{where } \lambda = \frac{y_1 - y_2}{x_1 - x_2} \pmod{p}. \end{aligned}$$

If $x_1 = x_2$ and $y_1 = y_2 \neq 0$, then we will define point Q3 coordinates in the following way:

$$\begin{aligned} | & x_3 = \lambda^2 - x_1 * 2 \pmod{p}, \\ | & y_3 = \lambda * (x_1 - x_3) - y_1 \pmod{p}, \\ & \text{where } \lambda = \frac{3 * x_1^2 + a}{y_1 * 2} \pmod{p}. \end{aligned}$$

If $x_1 = x_2$ and $y_1 = -y_2 \pmod{p}$, then the sum of points Q1 and Q2 is called a zero point O, without determination of its x- and y-coordinates. In this case, point Q2 is called a negative of point Q1. For the zero point, the equalities hold:

$$O + Q = Q + O = Q,$$

where Q is an arbitrary point of elliptic curve E.

A set of all points of elliptic curve E, including the zero point, forms a finite abelian (commutative) group of order m regarding the introduced addition operation. For m, the following inequalities hold:

$$p + 1 - 2 * \sqrt{p} \leq m \leq p + 1 + 2 * \sqrt{p}.$$

The point Q is called "a point of multiplicity k", or just "a multiple point of the elliptic curve E", if for some point P, the following equality holds:

$$\begin{aligned} Q &= P + \dots + P = k * P \\ &\quad \cdots \\ &\quad \quad k \end{aligned}$$

5. Protocol description

The protocol is used by subjects A and B that are commencing key establishment with password-based authentication.

5.1. Protocol parameters

Various elliptic curves can be used in the protocol. For each elliptic curve supported by clients the following values must be defined:

- o the curve identifier ID_ALG, that is a byte string of arbitrary length;
- o the point P, that is a generator point of the subgroup of order q of the curve;
- o the set of distinct curve points $\{Q_1, Q_2, \dots, Q_N\}$ of order q, where the total number of points N is defined for protocol instance.

The method of generation of the points $\{P, Q_1, Q_2, \dots, Q_N\}$ is described in Section 6.

The protocol parameters that are used by subject A are the following:

1. The secret password value PW, which is a byte string that is uniformly randomly chosen from a subset of cardinality 10^{10} or greater of the set B_k, where $k \geq 6$ is password length.
2. The list of curve identifiers supported by A.
3. Sets of points $\{Q_1, Q_2, \dots, Q_N\}$, corresponding to curves supported by A.
4. The C_1^A counter, that tracks the total number of unsuccessful authentication trials in a row, and a value of CLim_1 that stores the maximum possible number of such events.
5. The C_2^A counter, that tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of CLim_2 that stores the maximum possible number of such events.

6. The C_{3^A} counter, that tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of CLim_3 that stores the maximum possible number of such events. The identifier ID_A of subject A (optional), a byte string of an arbitrary length.
7. The unique identifier ID_A of the subject A (optional, see. Note 2), which is a byte string of an arbitrary length.

The protocol parameters that are used by subject B are the following:

1. The values ind and salt, where ind is in $\{1, \dots, N\}$, salt is in $\{1, \dots, 2^{128}-1\}$.
2. The point Q_PW, satisfying the following equation:

$$Q_{PW} = \text{int}(F(PW, \text{salt}, 2000)) * Q_{ind}.$$

It is possible that the point Q_PW is not stored and is calculated using PW in the beginning of the protocol. In that case B has to store PW and points Q_1, Q_2, ..., Q_N.

3. The ID_ALG identifier of the elliptic curve used in the protocol.
4. The C_{1^B} counter, that tracks the total number of unsuccessful authentication trials in a row, and a value of CLim_1 that stores the maximum possible number of such events.
5. The C_{2^B} counter, that tracks the total number of unsuccessful authentication events during the period of usage of the specific PW, and a value of CLim_2 that stores the maximum possible number of such events.
6. The C_{3^B} counter, that tracks the total number of authentication events (successful and unsuccessful) during the period of usage of the specific PW, and a value of CLim_3 that stores the maximum possible number of such events. The identifier ID_B of subject B (optional), a byte string of an arbitrary length.
7. The unique identifier ID_B of the subject B (optional, see. Note 2), which is a byte string of an arbitrary length.

5.2. Initial values of the protocol counters

After the setup of a new password value PW the values of the counters must be assigned as follows:

- o $C_{1^A} = C_{1^B} = CLim_1$, where CLim_1 is in $\{3, \dots, 5\}$;

- o $C_2^A = C_2^B = CLim_2$, where $CLim_2$ is in $\{7, \dots, 20\}$;
- o $C_3^A = C_3^B = CLim_3$, where $CLim_3$ is in $\{10^3, 10^{3+1}, \dots, 10^5\}$.

5.3. Protocol steps

The described protocol consists of the following steps:

1. If any of the counters C_1^A, C_2^A, C_3^A is equal to 0, A finishes the protocol with an error that informs of exceeding the number of trials that is controlled by the corresponding counter.
2. A decrements each of the counters C_1^A, C_2^A, C_3^A by 1, requests open authentication information from B and sends the ID_A identifier.
3. If any of the counters C_1^B, C_2^B, C_3^B is equal to 0, B finishes the protocol with an error that informs of exceeding the number of trials that is controlled by the corresponding counter.
4. B decrements each of the counters C_1^B, C_2^B, C_3^B by 1.
5. B sends the values of ind , salt and the ID_{ALG} identifier to A. B also can OPTIONALLY send the ID_B identifier to A. All following calculations are done by B in the elliptic curve group defined by the ID_{ALG} identifier.
6. A sets the curve defined by the received ID_{ALG} identifier as the used elliptic curve. All following calculations are done by A in this elliptic curve group.
7. A calculates the point $Q_{PW^A} = \text{int}(F(PW, salt, 2000)) * Q_{ind}$.
8. A chooses randomly (according to the uniform distribution) the value alpha, alpha is in $\{1, \dots, q-1\}$, and assigns $z_A = 0$.
9. A sends the value $u_1 = \alpha * P - Q_{PW^A}$ to B.
10. After receiving u_1 , B checks that u_1 is in E. If it is not, B finishes with an error, considering the authentication process unsuccessful.
11. B calculates $Q_B = u_1 + Q_{PW}$, assigns $z_B = 0$ and chooses randomly (according to the uniform distribution) the value betta, betta is in $\{1, \dots, q-1\}$.

12. If $m/q^*Q_B = 0$, B assigns $Q_B = P$ and $z_B = 1$.
13. B calculates $K_B = \text{HASH}((m/q^*\beta^*(\text{mod } q))^*Q_B)$, where the input of a hash function is a little-endian representation of the obtained point (x-coordinate first, then y-coordinate).
14. B sends the value $u_2 = \beta^*P + Q_{PW}$ to A.
15. After receiving u_2 , A checks that u_2 is in E. If it is not, A finishes with an error, considering the authentication process unsuccessful.
16. A calculates $Q_A = u_2 - Q_{PW}^A$.
17. If $m/q^*Q_A = 0$, then A assigns $Q_A = P$ and $z_A = 1$.
18. A calculates $K_A = \text{HASH}((m/q^*\alpha(\text{mod } q))^*Q_A)$, where the input of a hash function is a little-endian representation of the obtained point (x-coordinate first, then y-coordinate).
19. A calculates $\text{MAC}_A = \text{HMAC}(K_A, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2 || \text{DATA}_A)$, where DATA_A is an optional string that is authenticated with MAC_A (if it is not used, then DATA_A is considered to be of zero length).
20. A sends $(\text{DATA}_A || \text{MAC}_A)$ to B.
21. B checks that the values MAC_A and $\text{HMAC}(K_B, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2 || \text{DATA}_A)$ are equal. If they are not, it finishes with an error, considering the authentication process unsuccessful.
22. If $z_B = 1$, B finishes, considering the authentication process unsuccessful.
23. B sets the value of C_1^B to CLim_1 and increases C_2^B by 1.
24. B calculates $\text{MAC}_B = \text{HMAC}(K_B, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2 || \text{DATA}_A || \text{DATA}_B)$, where DATA_B is an optional string that is authenticated with MAC_B (if it is not used, then DATA_B is considered to be of zero length).
25. B sends $(\text{DATA}_B || \text{MAC}_B)$ to A.
26. A checks that the values MAC_B and $\text{HMAC}(K_A, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2 || \text{DATA}_A || \text{DATA}_B)$ are equal. If they are not, it finishes with an error, considering the authentication process unsuccessful.

27. If $z_A = 1$, A finishes, considering the authentication process unsuccessful.

28. A sets the value of C_1^A to $CLim_1$ and increases C_2^A by 1.

After the successful finish of the procedure the subjects A and B are mutually authenticated and each subject has an explicitly authenticated value of $K = K_A = K_B$.

Note:

1. In the case where the interaction process can be initiated by any subject (client or server) the ID_A and ID_B options MUST be used and the receiver MUST check that the identifier he had received is not equal to his own, otherwise, it finishes the protocol. If an optional parameter ID_A (or ID_B) is not used in the protocol, it SHOULD be considered equal to a fixed byte string (zero-length string is allowed) defined by a specific implementation.
2. The ind , ID_A , ID_B and salt parameters can be agreed in advance. If some parameter is agreed in advance, it is possible not to send it during a corresponding step. Nevertheless, all parameters MUST be used as corresponding inputs to HMAC function during stages 19, 21, 24 and 26.
3. The ID_ALG parameter can be fixed or agreed in advance.
4. Continuation of protocol interaction in case of any of the counters C_1^A , C_1^B being equal to zero MAY be done without changing password. In this case these counters can be used for protection against denial-of-service attacks. For example, continuation of interaction can be allowed after a certain delay.
5. Continuation of protocol interaction in case of any of the counters C_2^A , C_3^A , C_2^B , C_3^B being equal to zero MUST be done only after changing password.
6. Construction of points Q_1, \dots, Q_N

This section provides an example of possible algorithm for generation of each point Q_i in the set $\{Q_1, \dots, Q_N\}$ that corresponds to the given elliptic curve E.

The algorithm is based on choosing points with coordinates with a known preimages of a cryptographic hash function H, which is the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output, if $2^{254} < q < 2^{256}$, and the GOST R 34.11-2012 hash function (see [RFC6986]) with 512-bit output, if $2^{508} < q < 2^{512}$.

The algorithm consists of the following steps:

1. Choose an arbitrary SEED value with length of 32 bytes or more.
2. Calculate $X = \text{INT}(H(\text{SEED})) \bmod p$.
3. Check that the value of $X^3 + aX + b$ is a quadratic residue in the field F_p . If it is not, return to Step 1.
4. Choose the value of Y arbitrarily from the set $\{+\sqrt{A}, -\sqrt{A}\}$, where $A = X^3 + aX + b$. Here \sqrt{A} is an element of F_p , for which $(\sqrt{A})^2 = A \bmod p$.
5. Check that for point $Q = (X, Y)$ the following relations hold: $Q \neq O$ and $q*Q = O$. If they do not, return to Step 1.

With the defined algorithm for any elliptic curve E point sets $\{Q_1, \dots, Q_N\}$ are constructed. Constructed points in one set MUST have distinct x-coordinates.

Note: The knowledge of hash function preimage prevents knowledge of the multiplicity of any point related to generator point P . It is of primary importance, because such a knowledge could be used to implement an attack against protocol with exhaustive search of password.

7. Acknowledgments

We thank Lolita Sonina, Georgy Borodin, Sergei Agafin and Ekaterina Smyshlyaeva for their careful readings and useful comments.

8. Security Considerations

Any cryptographic algorithms, particularly HASH function and HMAC function, that are used in the SESPKE protocol MUST be carefully designed and MUST be able to withstand all known types of cryptanalytic attack.

It is RECOMMENDED that the HASH function satisfies the following condition:

$\text{hashlen} \leq \log_2(q) + 4$, where hashlen is the the lengths of the HASH function output.

The output lengths of hash functions that are used in the SESPKE protocol is RECOMMENDED to be greater or equal to 256 bits.

The points Q_1, Q_2, \dots, Q_3 and P must be chosen in such a way that they are provable pseudorandomness. As a practical matter, this

means that the algorithm for generation of each point Q_i in the set $\{Q_1, \dots, Q_N\}$ (see Section 6) ensures that multiplicity of any point under any other point is unknown.

9. Normative References

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Appendix A. Test examples for GOST-based protocol implementation

The following test examples are made for the protocol implementation that is based on the Russian national standards GOST R 34.10-2012 [GOST3410-2012] and GOST R 34.11-2012 [GOST3411-2012]. The English versions of these standards can be found in [RFC7091] and [RFC6986].

A.1. Examples of points

There are three points (Q_1 , Q_2 , Q_3) for each of the elliptic curves below. These points were constructed using the method described in Section 6, where the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output is used if $2^{254} < q < 2^{256}$ and the GOST R 34.11-2012 hash function (see [RFC6986]) with 512-bit output is used if $2^{508} < q < 2^{512}$.

The same method should be used for constructing, if necessary, additional points. Each of the points complies with the GOST R 34.10-2012 [GOST3410-2012] standard and is represented by a pair of (X , Y) coordinates in the canonical form and by a pair of (U , V) coordinates in the twisted Edward form in accordance with the document [RFC7836] for the curves that have the equivalent representation in this form. There is a SEED value for each point, by which it was generated.

A.1.1 Curve id-GostR3410-2001-CryptoPro-A-ParamSet

Point Q_1

$X = 0xa33ce065b0c23e1d3d026a206f8a1f8747ed1cd92a665bf85198cdb10ac90a5c$

$Y = 0xb00d0dc0733883f05de9f55fd711f55998f5508cc40bead80c913b4d5b533667$

SEED:

```
f8 18 95 b4 13 69 d9 08 9e 3d 3c 56 e8 70 ba 5e
9d 55 5e 20 eb d9 c7 22 66 10 6d 79 c2 83 48 b8
ce 63 70 52 9a 82 9f 18 a4 d3 e3 fd 7b f2 dd 73
b1 1b bc d4 10 9d 27 c9 a3 d4 bd 3a 42 cc 26 ae
43 5b 52 f5 89 a4 c3 b7 61 c0 1b a2 88 b7 e0 8d
f9 4e 22 40 29 f3 aa 96 11 5c 43 f5 eb 87 99 70
```

Point Q_2

$X = 0x4ce9c2bcf17212b9efcab65c3c815c0ff96d7461c957634dbfd1fe7c9a324d27$

$Y = 0xf7500d7adea2c2b4a16d838a8faa02b46639eb881f124d0f2506efca0e24289d$

SEED:

```
fd 99 6d bc c7 2e 49 a4 37 e7 49 a8 85 ad de 28
```

```

4b 58 64 bd 3b 7e 60 fc b5 2f c8 36 0e 0a bf 98
fd 35 7a 3f 98 c5 f6 20 c8 68 3d b2 ca b9 27 b6
13 f2 91 a1 52 45 c0 65 71 dc 62 b0 4f 2e e5 76
56 a9 fa 51 12 23 5d 0b 80 67 59 af e2 33 b1 09
6a 94 84 91 45 f2 18 50 65 b7 9b 86 ab 68 8a 39

```

Point Q_3

X= 0x31fb8e5070b1e0f52f047f40477c38c6020fd8da9f685791f9237cc47bd89324

Y= 0x8ba1184a4e296dc5c5873639747339ecc71b7fa44d31cc8e35b6615a4f797dd7

SEED:

```

29 0c 12 66 47 91 2e de 11 cc 43 78 0c f8 87 d4
7d a1 63 bc fb 91 1d 92 86 2a ae 4f 53 a6 80 70
08 c1 ec 0c 8f e7 2e 0a a0 81 df a3 32 7c 86 ad
5f 24 da 28 a7 1d 07 f5 fd b7 61 31 a1 fb 04 d5
b2 31 c7 7f ca 26 d3 a6 42 99 9e 3b 10 74 b5 a7
b3 54 2f 03 b0 39 63 2a 6b 44 56 36 fb 52 8d 58

```

A.1.2 Curve id-GostR3410-2001-CryptoPro-B-ParamSet

Point Q_1

X= 0x0ad754474a915d9d706c6b8dc879858a1cb85cc8f6c148fc3120825393ecd394

Y= 0x68c33b6d0343cf72cb19666ffd487fa94294dc677b28c8e27ec36068ff85ed83

SEED:

```

78 1d 7d 85 ff 04 12 b9 92 a7 6e 65 37 dd 83 81
9b 81 2f fa bf e8 92 3c d0 12 fe dc 00 c4 96 69
f6 52 44 4d 38 9a f2 b2 6f 57 b5 3e 2d 0f 81 2e
db 2c f3 d6 a7 18 42 52 32 da 47 18 75 1e ec ef
8f 2b c5 03 17 fb 49 6f 02 05 d7 99 bc 3c 34 87
12 f5 1b d3 ef aa 7f f5 ba c2 52 07 80 46 34 77

```

Point Q_2

X= 0x1cd96e72fdf1ce6b544dec12d0d7bcb9f6ba65bba3d9f7af732bcb133c1b6437

Y= 0x34ab5b63c286a2b885ca443ac875a8f9ec0c2f148f1622bc64c83b80e6e3d31f

SEED:

```

62 93 40 15 63 0c 9a 09 ce 76 32 6c fd 1c 04 36
ee 08 bc 92 b9 c0 3a d9 63 c6 db 00 18 12 12 fa
e0 1a 46 38 8b b6 81 df ae 4f 64 3e cc 0c 93 8c
e4 10 36 2f d9 6d 5c fd 99 f3 9c 13 fd 30 52 a1
3e 8b 35 8b ed 1c 31 b0 39 9c 03 dc 5a 94 2b 41
f8 ff 9d 62 41 bd eb 9d bf cf 54 b6 c8 cc d1 06

```

Point Q_3

X= 0x18dda7154e5abef001dc9943554439cb44b9e26256def176849da5f09b5f690d

Y= 0x3ef584be59673d1751b2fd6e3fdc619e3d756c0d355595b3a62196de048ece44

SEED:

```

33 17 39 c1 38 82 98 88 14 68 83 c6 97 14 86 8c
d0 d2 1a 28 41 51 99 a9 33 40 15 0b 30 88 35 01
4a 41 42 f8 d8 9a a6 bd e1 a6 81 23 94 19 e8 a0
ef 3d 36 02 ef ff 38 e6 10 4b 11 2f 7b b5 50 42
5a 7b 39 a6 00 53 1a 92 fc cc 2b 0d 95 dd ea 95
42 d4 27 6f a8 0f ae 45 b2 d6 f4 38 c1 52 17 5d

```

A.1.3 Curve id-GostR3410-2001-CryptoPro-C-ParamSet

Point Q_1

X= 0x339f791f62938871f241c1c89643619aa8b2c7d7706ce69be01fddff3f840003

Y= 0x31d6d9264cc6f8fe09bf7aa48910b4ad5ddf74a2ef4699b76de09ffed295f11

SEED:

0e	29	35	9d	45	dd	a3	b4	57	9b	17	e8	87	d9	9e	63
b9	d6	04	e3	ac	74	83	11	91	2a	5b	d4	86	7b	5d	9c
5d	07	70	64	cd	f1	2d	93	f7	f0	2e	f0	0a	e1	7b	8b
c1	87	50	b3	8f	39	bb	95	68	21	5c	42	e2	4e	8c	fe
59	e9	0f	a6	05	0b	76	68	a2	94	da	5f	2c	9a	27	28
1f	3a	7e	4e	14	54	10	21	01	6f	2c	a2	97	77	94	12

Point Q_2

X= 0x80f4d03b00b1b9b53f6bb4ffa52be65a6d316de846e27f44cccd795bc62d89e23

Y= 0x38dd712518ddec19b46afccccba97338d89d1292427dc12985d4e848066cd1ab

SEED:

f5	61	4e	92	8f	e5	5c	77	26	37	ab	ac	1b	1e	3c	dd
2a	37	77	be	25	23	cc	58	9a	79	5a	60	28	db	9e	64
f8	62	73	01	98	3e	dd	23	0b	eb	07	3e	81	9b	cb	d9
94	bc	bf	7f	9e	5f	e1	8f	a5	8a	ce	9e	f2	99	0e	9d
fb	ee	1c	64	38	22	33	c3	1b	e7	05	9e	c2	e9	bb	46
b9	dc	15	19	9d	e0	9f	cb	65	d5	6d	46	2f	01	21	65

Point Q_3

X= 0x0c8b64c3f0ec7ece81b6232db2e8054666d051ee28254d4b9a4bcb1460ca546b

Y= 0x88c98b48b22b90d0d3a018da55ca0d05cedd82b6c838bd62aba2b823ce82b28f

SEED:

8a	1b	29	62	38	f5	c2	e2	9b	4a	c0	5b	6d	57	99	88
86	69	a4	1b	b9	f6	60	f3	a3	15	26	e5	f4	33	1e	ae
80	9a	38	52	f5	44	86	91	71	76	1c	ab	77	0a	b6	2e
c3	6f	d6	4d	3c	31	a3	67	2a	82	25	bf	d6	ae	c9	95
66	95	b8	87	39	6a	3e	bf	ef	28	65	16	b9	51	29	1d
65	df	12	7a	eb	4c	ec	f1	6f	08	f5	98	36	0a	b9	a0

A.1.4 Curve id-tc26-gost-3410-2012-512-paramSetA

Point Q_1

X= 0x301aac1a3b3e9c8a65bc095b541ce1d23728b93818e8b61f963e5d5b13eec0fe
e6b06f8cd481a07bb647b649232e5179b019eef7296a3d9cfab66ee8bf0cbf2Y= 0x191177dd41ce19cc849c3938abf3adaab366e5eb2d22a972b2dcc69283523e89
c9907f1d89ab9d96f473f96815da6e0a47297fcdd8b3adac37d4886f7ad055e0

SEED:

64	1c	90	19	c5	d7	68	91	de	d1	9a	31	28	4e	7c	d3
c6	8b	74	e5	e6	a7	20	b5	2c	fb	45	17	9f	91	b3	f6
3a	0c	b2	5e	3f	91	e3	eb	80	3d	80	4f	79	98	a3	57
f2	e5	dc	5d	84	ab	d6	7d	33	a3	2b	89	66	db	c6	94
96	8f	96	2d	37	9e	33	c0	fd	14	32	dd	02	70	fb	61
1a	88	4c	6d	ae	1b	58	20	24	6e	80	80	5d	cd	a8	66

Point Q_2

X= 0x7edc38f17f88e3105bafb67c419d58fe6a9094dd4dc1a83bcaccc61f020ac447
92eba888457c658ee2d82557b7c6ab6efd61ba0c3327741d09a561a8b860a085

$Y = 0x3af1400a7a469058d9ba75e65ea5d3f4d0bdb357fa57eb73fa4900e2dca4da78b8e5ff35ca70e522610bb1fc76b102c81cc4729f94b12822584f6b6229a57ea1$

SEED:

```
3d ad a1 b4 fb 87 3e 13 1e 51 62 60 1f ee f1 54
b0 77 e0 71 1b cf da 74 a2 20 7e a3 20 01 c3 f5
79 00 5f 10 9f c1 83 83 4e 29 46 b3 29 8a 4c 10
0c 69 f4 c6 40 92 3f ed af b2 68 08 0b 6b 1c 07
48 a1 18 29 6e 64 9b f6 1d eb 26 27 b4 77 9e e8
e0 ff c1 db 48 5d 8b c1 10 8c 58 b1 af 07 5f 7b
```

Point Q_3

$X = 0x387acfba7bbc5815407474a7c1132a1bded12497243d73ef8133d9810eb2171695dde2ff15597e159464a1db207b4d1ff98fb989f80c2db13bc8ff5fea16d59$

$Y = 0x4c816d1ca3e145ac448478fb79a77e1ad2dfc69576685e2f6867ec93fbad8aa44111acd104036317095bce467e98f295436199c8ead57f243860d1bde8d88b68$

SEED:

```
7c 8d a6 91 96 0d 9d 06 65 92 23 08 df cf 51 71
bd 7c 4b f8 50 1b 3f fd 3c b1 58 3a 30 e1 a7 17
4e 09 e2 5f 1d 19 35 6e b0 51 66 1c d0 2a c1 9e
48 22 38 49 76 0d 43 4e 20 ea d1 80 73 84 1c e8
36 a6 8e f3 24 bb 2d 57 45 32 a5 d4 e6 08 73 fa
d3 8c 32 e8 af a1 c5 25 8c ff 3d 52 ca ac 98 d1
```

A.1.5 Curve id-tc26-gost-3410-2012-512-paramSetB

Point Q_1

$X = 0x488cf12b403e539fde9ee32fc36b6ed52aad9ec34ff478c259159a85e99d3dda9fd5d73606ecee351e0f780a14c3e9f14e985d9d7ddc93b064fc89b0c843650$

$Y = 0x7bc73c032edc5f2c74dd7d9da12e1856a061ce344a77253f620592752b1f3a3dcbbbc87eb27ec4ed5e236dfcb03f3972404747e277671e53a9e412e82aaaf6c3f7$

SEED:

```
40 57 8b 1a c0 bd 53 8d 75 97 2d 49 9b 1c c6 73
94 c8 f7 d4 76 cd fe 15 59 02 fa 0f 28 b8 06 e1
81 4c fb d0 4d 62 86 0c 4a ce c1 0e 88 13 da 2a
d4 fd 7a 13 4d ba 75 0d 2c 80 f2 68 ba c1 b4 34
98 ea fe 10 51 86 60 b7 70 30 f8 64 6f 21 d9 40
aa da 62 3e ad 44 3f 93 73 a5 6b c3 15 55 3c bd
```

Point Q_2

$X = 0x175166b97248bda12ec035df2e312a2771d0b16977c9cbc79461ff05e01f719c92ae8b53f3b7e3edcacffcc5063b5e9c8de18d0cb87da358350992132173df69$

$Y = 0x10e2943dc1a18a841ab76ac756fa974948d5a18d071d458a4769c2494fe2a6c5966e3c8931e624d87259156aea9317157502698e4a4a489c327b89277cf59b4c$

SEED:

```
26 01 07 1b 3d 3e 6d e7 0e d0 22 ae be 81 be 47
51 77 49 b6 5d 29 d1 07 5c df cb f4 56 a8 77 54
2b e9 91 50 34 06 b3 aa 71 c5 ce 16 b6 5f e9 93
e7 48 99 58 b1 26 81 10 9f 9b e4 30 38 73 77 13
f0 6a 4f 30 05 b2 66 76 9f b8 1b 5f 39 55 52 97
ab 46 6b 5d 2e 19 2d 12 f3 2a b3 18 72 71 52 62
```

Point Q_3

X= 0x01f4583db894cdebd7c591af848783ee011a20567751ca1561f398a6118ace08
 a4efef1501bda67f39d060270ba660526dc53063c6b40fa5548c9a9e7688f2239
 Y= 0x7bc640641d70c8296bd9257c9eebb5b1bd3196a169bac04f7579bf27b5847d4e
 7b4f63748ad81b5469070ed35ad93e5a5258652306f84094eae04a91954536ee

SEED:

bb	9a	63	a5	67	7d	40	7c	f3	4d	06	df	96	7d	d9	e9
ca	4d	42	eb	d6	7d	a5	69	a4	9b	d8	b1	04	64	2e	20
fb	a9	9d	84	2f	cb	54	76	61	dc	7a	a4	de	72	6f	67
4a	09	85	46	20	04	7c	c1	75	2c	ab	67	99	8b	5c	8e
6a	88	6d	0a	06	e6	a3	fa	e8	19	34	21	1a	ec	81	8d
89	03	9e	45	dc	a1	85	03	7e	c3	49	37	33	ee	3c	2e

A.1.6 Curve id-tc26-gost-3410-2012-256-paramSetA

Point Q_1

X= 0x5161b08a973d521bdde0cbd45b68aa0470e1058dd936e5bd618fd3373770eed9
 Y= 0xc1633db551677c62b9c2b69d47e503c0f8ca83b6b3109dece0a5f985d77a83a7
 U= 0x9c5ad63ddc3314ac009d879780d6219720bf4573f4fe6b4bf7a0a88860677f9d
 V= 0x8ee071a767f3d6f0435eb6100d1a936f984e43d9af0bc91a864a9e65cee025fb

SEED:

c4	7e	5e	42	31	4e	dd	8e	e9	ac	39	fb	c8	da	ea	c8
e6	5b	fd	26	58	27	4e	1f	99	e9	33	e1	1e	5d	f2	62
4a	e3	97	f1	7e	db	f9	83	60	f3	ec	2e	8f	6f	2e	ff
d4	aa	80	5c	71	d6	ed	5b	a1	5b	c9	d0	ad	d6	38	23
84	c1	55	20	a5	b8	bb	bd	7b	23	1f	c8	fb	8c	77	71
57	b9	77	25	91	55	3f	17	46	8c	4b	b3	64	6f	9f	53

Point Q_2

X= 0xd47abd59dccad35849dec9dc721ffale44419ca8686406a9f441e61294b210ed
 Y= 0xa78b64220bf3375d08de0ea5e2920cf8f204da6757bf1878ac870fb7e5ca0e8
 U= 0xf0195efb6b249eb8018c19376907c787511bf30516a5c27d045fc7ba2af58ed0
 V= 0xacae88466127df000b663863bc7bd394eafa6996fcedad11d7834f502a6a2686

SEED:

30	5f	d0	bb	ce	c7	16	49	ac	e4	1b	4d	ca	07	6c	a6
96	a8	8c	c6	fd	06	91	a8	79	13	5d	e1	90	96	e3	c8
03	c5	b4	ad	41	68	36	9b	e7	b9	ed	81	d6	e2	bd	0c
a2	8e	b0	e9	6f	74	2d	50	e2	df	b6	a1	86	ae	15	60
96	a3	5a	97	a2	20	fa	6d	0f	cf	88	db	6d	86	cd	db
19	7c	3a	21	5f	10	cc	ea	42	95	ef	aa	b2	63	95	d5

Point Q_3

X= 0xe0d610ff42ce21eb308980964ca368963fbe5cb08c277187d22d0c94f4bf0762
 Y= 0x82619b88da25b666e07b617ff487be8afdf5af8b092568b493ecef44ee0c04b5f
 U= 0x723df0719311d095b814ee05ca086e18c410c375a48789dc03c3fe844ed3b7c9
 V= 0x160e1b5338337ee0620745206dbe5556a7ff5d19735418a3cc03bf7f2735ce25

SEED:

22	16	91	c7	21	8d	93	d4	a8	ad	15	e4	72	33	84	90
ca	5c	5e	3b	84	84	57	4e	bc	df	83	26	68	84	5e	f4
09	53	71	79	7a	f8	e2	a6	e3	99	93	de	2a	7c	65	f0
37	26	2e	cc	fa	95	58	9a	c6	e8	b1	2d	e6	09	af	be

```
f9 2f 12 d0 a3 08 56 9a b3 c0 fa d8 ec 5d 7b 9c
f4 27 1f aa 54 bc bb da 31 61 b7 cd f5 40 d6 b8
```

A.1.7 Curve id-tc26-gost-3410-2012-512-paramSetC

Point Q_1

```
X= 0x5b065ead2e94de0ee2e462de204c93c6b2bf3498ad920393cb60259e1a8ffc7c
    7e7d4defa20ff4282abf70207e4611d532f40db6800e29d2b53f6ac0713e5b38
```

```
Y= 0xa39a28c59ff7f796b85223b8834384907c626086415487288ed1182ca4487dc1
    ae5f37af90fd267b7c0dc8542ea52cd984af54731bc84271d6186d973c91359b
```

```
U= 0x3c80e89805380f52cf86ff990501801d70e5b4636e8478674d2d5706a56a666
    63eb03abdc332584f7ea8c3255b1be3ca75e4685a060e0ea88e569612d9e7227
```

```
V= 0xd8f2cf17c484f4bb6a0208b3796a2609971c55d56bffadf155c0bf76f7afe99
    7d6b6e8fde9e2cefd0ab3e31a1862953425a70334e4e2404c9cd9079856c7259
```

SEED:

```
03 8a 01 b5 ea a2 28 3b bb 29 7b 81 ad 94 92 01
e4 32 11 df 76 a3 70 ec c0 09 ec 49 1f 9f 8d 33
f2 ee 24 08 c7 88 27 cd 0c 51 17 a7 e3 8d 58 5b
3d 15 50 30 a3 29 1b ad 6a 21 ab 48 38 1d 66 bc
1b d6 b9 ba 6e d8 6a 21 65 c5 99 84 dc 5d 51 81
f3 f1 97 fe 4a 86 81 c2 e5 0a 22 a0 61 2c 55 7e
```

Point Q_2

```
X= 0xb3e6c475f173af4494dd02ad7c9df3bd6a5ca82c3d65ad86fb330dfb1c40e34
    c4cd04d93f609cff2daea5907d0e08192a29be3ff2752223b868e8bcc6a7b74
```

```
Y= 0x53ffcf818281bcf383d9b6542b3b1fce5bd20cd1c805ed1dacb83ba161167a5
    eb96df52c1d290496043ea514c465ecb37970fcf7ffbb6ca35a767cd0227fe8c
```

```
U= 0x8dd3f6f455ffaea85c3935750792b65fa1ba990c7ac8bc449a77bb86aeb87eb6
    ecb6bf387924885b0ea1e30fc4d742919504cd7baf4926b777ed40b898be41f8
```

```
V= 0x2d7edc1ca6078878d2d8ecafabc2abc83fc269c049baa11951ff2523b69b1d1
    4ee6c0fa7cbd5a566cb32246d14568eb9fa04e3b53ee6175bb32887796870ba9
```

SEED:

```
63 ce db 44 3d f8 df 68 8d 5d fd d0 ea 54 41 62
f5 6d 78 92 73 0c 86 88 53 e2 24 4d dd 87 1e 4a
0e 3f b7 32 40 c8 7a bc e8 fd b3 16 dd 0e 9b 23
ec 1f c7 40 86 29 8c fc f2 a1 d9 18 31 af a3 cf
1e 98 b8 0d 42 0c f6 73 8d 57 44 77 8e 1a d3 e4
42 d7 26 39 6c 91 b7 f5 e8 84 09 8d be 02 aa 80
```

Point Q_3

```
X= 0xbe963ad90f84ff9ff6ff7ddd39d91cea649e849bf20b8cc1e72040cf689a974f
    40f24e10c737bfa558b514c605b7c156e24251b859202b12ef311b0f363171eb
```

```
Y= 0x007cfa56f5ae239694e74f7996e1f44fc4f62205a555fdb627e4212576b4591
    7f88667bcd924a3271f40dc4bbd2f2e216b4fcf59c25fdd8154241d40f42e2ad
```

```
U= 0xff6697883ce5c6cc165fa78ff158c03b31add23dc01b24902b18c5487f1835ff
    eaf4af5ede44f8b254748704e504810597d0e4418daf50e0253f33915de97b7b
```

```
V= 0x54e1ba656234479c5845c06af70bbeafa741a863d5186ca720ee2f43bdd4d5b74
    71594871d532ce263928aa30ae3c25efc6a2f82d4163c45869339426888be3bc
```

SEED:

```
06 ce 08 fa 5d 11 50 45 e2 d2 a8 03 01 d2 9e 2a
39 c3 ea e7 f1 61 37 f9 3e 51 d1 46 f3 21 b1 89
```

```

fb 5c 17 70 26 5b 30 8b 6d f2 87 7c d9 d3 6f 8a
3c b4 e7 1d f0 99 a4 73 69 1d d5 46 8d 43 50 f9
87 df e5 e5 de ff 3c 7b b8 f4 62 ed 19 9b f3 33
7a 6f f9 0e c5 f0 bc bb 1a 59 1e cd c2 9b 52 64

```

A.2. Test examples

This protocol implementation uses the GOST R 34.11-2012 hash function (see [RFC6986]) with 256-bit output as the H function and the HMAC_GOSTR3411_2012_512 function defined in [RFC7836] as a PRF function for the F function. The parameter len is considered equal to 256, if $2^{254} < q < 2^{256}$, and equal to 512, if $2^{508} < q < 2^{512}$.

The test examples for one of the three points of each curve in Appendix A.1 of this document are given below.

A.2.1 Curveid-GostR3410-2001-CryptoPro-A-ParamSet

The input protocol parameters in this example take the following values:

```

N= 3
ind= 1
ID_A:
  00 00 00 00
ID_B:
  00 00 00 00
PW:
  31 32 33 34 35 36 ('123456')
salt:
  29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
Q_ind:
  X= 0xa33ce065b0c23e1d3d026a206f8a1f8747ed1cd92a665bf85198cdb10ac90a5c
  Y= 0xb00d0dc0733883f05de9f55fd711f55998f5508cc40bead80c913b4d5b533667

```

The function F (PW, salt, 2000) takes the following values:

```

F(PW,salt,2000):
  bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
  d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67

```

The coordinates of the point Q_PW are:

```

X= 0x9d339b3396ae4a816388a14c79ab3a8dd495fa4c53f0d4076579022ef2aaeb68
Y= 0xdad91482e208590fd316bf959480f5ec2c17463ec8fc8f63030649b452cddda8

```

During the calculation of the message u_1 on the subject A the parameter alpha, the point alpha*P and the message u_1 take the following values:
alpha=0xfcdb45d1f2538097d5a031fa68bbb43c84d12b3de47b7061c0d5e24993e0c87
alphaP:

```

X= 0x24538e096781b9d53316c342ae5bbd49ccfb2db627c3659175bc4fa9d95b4618
Y= 0xf6e39a7490ae0ac449f5abe7e2135697c582daf3a038c40a05e6e8be3e466a2b

```

```

u_1:
  X= 0xcf73b30dd577369fb98e2a93d6d98d7450f9ceef2badale3dcbb1016dff1e1
  Y= 0x1cf05014caedb1635120b30e0a445060b8f1cca52965cf83c4838d554ca4e2

```

During processing a message u_1 , calculation the K_B key and the message u_2 on the subject B the parameters betta, src, $K_B = \text{HASH}(\text{src})$, betta^*P and u_2 take the following values:

$\text{betta}=0xf2144faddc497d9ef6324912fd367840ee509a2032aedb1c0a890d133b45f596$
 $\text{src}:$

```
39 c0 e8 83 59 91 cd 6d 56 88 fc ad 55 29 1f 79
e5 0f 87 9d 94 b5 0a b2 db d6 bd f7 e8 39 b7 1a
10 b5 a7 8d c0 36 b8 73 f7 e4 b1 6b 12 48 6f eb
69 d7 39 d4 01 4d ae e2 cc 5c 2f c7 4a 2c c8 06
```

$K_B:$

```
e0 4e e0 14 7f 9f 19 8d e2 5a af 33 a2 84 99 e0
ce 7d 31 6e 47 39 76 2f d5 19 f8 e9 91 d7 fc 00
```

$\text{betta}^*P:$

```
X= 0xb11f1a8fb043bc6d4068667b897e4ff637b8410f5eb19e11b0a7028f34d6936a
Y= 0x266d952955e2ab3f3ba75d14a919795d6b8ac04dbcff1cfaac6ba32291c099fd
```

$u_2:$

```
X= 0x6e1bfb24b6131a3ad0b60e477a38715c6f96f21bb0b2f9ebd67680e804a77199
Y= 0x873ee3c546c41e8f707298f11b955fe64f7577d52d7adc1beccb9925178ca80
```

During processing a message u_2 and calculation the key on the subject A the the K_A key takes the following value:

$K_A:$

```
e0 4e e0 14 7f 9f 19 8d e2 5a af 33 a2 84 99 e0
ce 7d 31 6e 47 39 76 2f d5 19 f8 e9 91 d7 fc 00
```

The message $\text{MAC}_A=\text{HMAC}(K_A, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2)$ from the subject A takes the following value:

$\text{MAC}_A:$

```
bd 35 c5 0e 90 60 e6 4f 04 2e 7b e6 cc 02 99 84
0c 8e 27 82 b8 e5 9c 3d d4 47 50 11 16 73 c5 ea
```

The message $\text{MAC}_B=\text{HMAC}(K_B, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2)$ from the subject B takes the following value:

$\text{MAC}_B:$

```
c8 c8 2c 0f ed 8e 4d 1e 41 42 d7 a9 f0 55 b4 5f
f6 71 2d 2f 41 bf 26 ef 2f bc 37 c5 56 4b 86 d3
```

A.2.2 Curveid-GostR3410-2001-CryptoPro-B-ParamSet

The input protocol parameters in this example take the following values:

$N=3$

$\text{ind}=1$

$ID_A:$

```
00 00 00 00
```

$ID_B:$

```
00 00 00 00
```

$PW:$

```
31 32 33 34 35 36 ('123456')
```

$\text{salt}:$

```
29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
```

$Q_{\text{ind}}:$

```
X= 0xad754474a915d9d706c6b8dc879858a1cb85cc8f6c148fc3120825393ecd394
```

$Y = 0x68c33b6d0343cf72cb19666ffd487fa94294dc677b28c8e27ec36068ff85ed83$
 The function F (PW, salt, 2000) takes the following values:

$F(PW, salt, 2000) :$

```
bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67
```

The coordinates of the point Q_{PW} are:

$X = 0x7a7211a430fd4e31b815e6d2454eea9574f034c5c442dce1723d69555d3ee4c9$

$Y = 0x2995e857187808e80d3e40a00fb87128e203f2d91c1f15d8193a5aad95964734$

During the calculation of the message u_1 on the subject A the parameter alpha, the point $\alpha * P$ and the message u_1 take the following values:

$\alpha = 0x499d72b90299cab0da1f8be19d9122f622a13b32b730c46bd0664044f2144fad$
 $\alpha * P :$

```
X= 0x61d6f916db717222d74877f179f7ebef7cd4d24d8c1f523c048e34a1df30f8dd
Y= 0x3ec48863049cfcf662904082e78503f4973a4e105e2f1b18c69a5e7fb209000
```

$u_1 :$

```
X= 0x35e78fcbc24998eb3039445a9de7032aadf291e7768196ef618e45bed80edf88
Y= 0x1970a4697295f6d361d2c3edd3885794c1254bac3f4adb4a3346ad01a911d13c
```

During processing a message u_1 , calculation the K_B key and the message u_2 on the subject B the parameters betta, src, $K_B = \text{HASH}(\text{src})$, $\text{betta} * P$ and u_2 take the following values:

$\text{betta} = 0x0f69ff614957ef83668edc2d7ed614be76f7b253db23c5cc9c52bf7df8f4669d$
 $\text{src} :$

```
50 14 0a 5d ed 33 43 ef c8 25 7b 79 e6 46 d9 f0
df 43 82 8c 04 91 9b d4 60 c9 7a d1 4b a3 a8 6b
00 c4 06 b5 74 4d 8e b1 49 dc 8e 7f c8 40 64 d8
53 20 25 3e 57 a9 b6 b1 3d 0d 38 fe a8 ee 5e 0a
```

$K_B :$

```
a6 26 de 01 b1 68 0f f7 51 30 09 12 2b ce e1 89
68 83 39 4f 96 03 01 72 45 5c 9a e0 60 cc e4 4a
```

$\text{betta} * P :$

```
X= 0x33bc6f7e9c0ba10cfb2b72546c327171295508ea97f8c8ba9f890f2478ab4d6c
Y= 0x75d57b396c396f492f057e9222ccc686437a2aad464e452ef426fc8eed1a4a6
```

$u_2 :$

```
X= 0x20d7a92b238143e3f137be904d52fa35c45a29f02a7226a7ac83a1172c2a55cd
Y= 0x5fc4cd6ffb0e76ea8603ce9e6dab5164285617969ab3bfab09fbe8595d1f47b
```

During processing a message u_2 and calculation the key on the subject A the K_A key takes the following value:

$K_A :$

```
a6 26 de 01 b1 68 0f f7 51 30 09 12 2b ce e1 89
68 83 39 4f 96 03 01 72 45 5c 9a e0 60 cc e4 4a
```

The message $\text{MAC}_A = \text{HMAC}(K_A, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2)$ from the subject A takes the following value:

$\text{MAC}_A :$

```
55 7a 59 61 42 60 39 a1 52 c8 23 a7 65 04 59 b0
62 be 3d 47 56 53 03 09 95 57 1c e7 53 40 26 47
```

The message $\text{MAC}_B = \text{HMAC}(K_B, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2)$ from the subject B takes the following value:

$\text{MAC}_B :$

```
3b c5 5e 27 07 84 19 94 c4 b9 ca ba 43 e6 ce 6a
09 2d e9 08 83 76 5f b6 c3 44 c6 1d 76 02 96 e9
```

A.2.3 Curveid-GostR3410-2001-CryptoPro-C-ParamSet

The input protocol parameters in this example take the following values:

N= 3

ind= 1

ID_A:

```
00 00 00 00
```

ID_B:

```
00 00 00 00
```

PW:

```
31 32 33 34 35 36 ('123456')
```

salt:

```
29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
```

Q_ind:

```
X= 0x339f791f62938871f241c1c89643619aa8b2c7d7706ce69be01fddff3f840003
```

```
Y= 0x31d6d9264cc6f8fe09bf7aa48910b4ad5ddf74a2ef4699b76de09ffed295f11
```

The function F (PW, salt, 2000) takes the following values:

F(PW,salt,2000):

```
bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
```

```
d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67
```

The coordinates of the point Q_PW are:

```
X= 0xb666917d42c455331358c50c3c12c85b898a2e454b50dd773541da02e1c3068
```

```
Y= 0x8a9b6c4703934b7f0dc903f52c16275e1d38b568117c7cff3bd322a99a311fe9
```

During the calculation of the message u_1 on the subject A the parameter alpha, the point alpha*P and the message u_1 take the following values:

alpha=0x3a54ac3f19ad9d0b1eac8acdcea70e581f1dac33d13feaf81e762378639c1a8

alphaP:

```
X= 0x96b7f09c94d297c257a7da48364c0076e59e48d221cba604ae111ca3933b446a
```

```
Y= 0x54e4953d86b77ecceb578500931e822300f7e091f79592ca202a020d762c34a6
```

u_1:

```
X= 0x2124a22e00b1be2114f5ca42d58d55a0a9f2b08f8cb10275edd8243402abb7a
```

```
Y= 0x62497815861d15877b7ad2e86768a2deb0f755a8b1a8897fc5235da783914a59
```

During processing a message u_1, calculation the K_B key and the message u_2 on the subject B the parameters betta, src, K_B = HASH (src), betta*P and u_2 take the following values:

betta=0x448781782bf7c0e52a1dd9e6758fd3482d90d3cfccf42232cf357e59a4d49fd4

src:

```
16 a1 2d 88 54 7e 1c 90 06 ba a0 08 e8 cb ec c9
```

```
d1 68 91 ed c8 36 cf b7 5f 8e b9 56 fa 76 11 94
```

```
d2 8e 25 da d3 81 8d 16 3c 49 4b 05 9a 8c 70 a5
```

```
a1 b8 8a 7f 80 a2 ee 35 49 30 18 46 54 2c 47 0b
```

K_B:

```
be 7e 7e 47 b4 11 16 f2 c7 7e 3b 8f ce 40 30 72
```

```
ca 82 45 0d 65 de fc 71 a9 56 49 e4 de ea ec ee
```

betta*P:

```
X= 0x4b9c0ab55a938121f282f48a2cc4396eb16e7e0068b495b0c1dd4667786a3eb7
```

$Y = 0x223460aa8e09383e9df9844c5a0f2766484738e5b30128a171b69a77d9509b96$
 $u_2:$
 $X = 0x47ad0110d1620fe38832e90b58971d2e0b9183dd52de23422b6fc47bec64541a$
 $Y = 0x8296af496b3c52640e738a195d63ab7bfb457aba7c71b5649cc3e300829cbf0a$
 During processing a message u_2 and calculation the key on the subject A
 the K_A key takes the following value:
 $K_A:$

$be\ 7e\ 7e\ 47\ b4\ 11\ 16\ f2\ c7\ 7e\ 3b\ 8f\ ce\ 40\ 30\ 72$
 $ca\ 82\ 45\ 0d\ 65\ de\ fc\ 71\ a9\ 56\ 49\ e4\ de\ ea\ ec\ ee$
 The message $MAC_A = \text{HMAC}(K_A, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2)$
 from the subject A takes the following value:
 $MAC_A:$

$47\ 58\ fa\ 64\ 9f\ 2e\ 31\ 3b\ f2\ 70\ 8b\ 76\ a7\ f7\ a7\ 5a$
 $37\ ce\ 9e\ 7f\ 55\ c3\ fc\ 5a\ 55\ 77\ e8\ 77\ a7\ a2\ c1\ ea$
 The message $MAC_B = \text{HMAC}(K_B, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2)$
 from the subject B takes the following value:
 $MAC_B:$

$2f\ 33\ b9\ bf\ f0\ 7d\ cd\ e3\ 44\ 67\ bd\ b0\ 7f\ 62\ fc\ a8$
 $b3\ 52\ 3a\ 64\ 39\ ef\ f1\ c9\ 93\ ba\ 0b\ 4c\ e6\ c2\ ed\ e4$

A.2.4 Curveid-tc26-gost-3410-2012-512-paramSetA

The input protocol parameters in this example take the following values:

$N = 3$
 $\text{ind} = 1$
 $ID_A:$
 $00\ 00\ 00\ 00$
 $ID_B:$
 $00\ 00\ 00\ 00$
 $PW:$

$31\ 32\ 33\ 34\ 35\ 36\ ('123456')$
 $salt:$
 $29\ 23\ be\ 84\ e1\ 6c\ d6\ ae\ 52\ 90\ 49\ f1\ f1\ bb\ e9\ eb$
 $Q_{\text{ind}}:$

$X = 0x301aac1a3b3e9c8a65bc095b541ce1d23728b93818e8b61f963e5d5b13eec0fe$
 $e6b06f8cd481a07bb647b649232e5179b019eeff7296a3d9cfab2b66ee8bf0cbf2$
 $Y = 0x191177dd41ce19cc849c3938abf3adaab366e5eb2d22a972b2dcc69283523e89$
 $c9907f1d89ab9d96f473f96815da6e0a47297fcdd8b3adac37d4886f7ad055e0$

The function $F(PW, salt, 2000)$ takes the following values:

$F(PW, salt, 2000):$
 $bd\ 04\ 67\ 3f\ 71\ 49\ b1\ 8e\ 98\ 15\ 5b\ d1\ e2\ 72\ 4e\ 71$
 $d0\ 09\ 9a\ a2\ 51\ 74\ f7\ 92\ d3\ 32\ 6c\ 6f\ 18\ 12\ 70\ 67$
 $1c\ 62\ 13\ e3\ 93\ 0e\ fd\ da\ 26\ 45\ 17\ 92\ c6\ 20\ 81\ 22$
 $ee\ 60\ d2\ 00\ 52\ 0d\ 69\ 5d\ fd\ 9f\ 5f\ 0f\ d5\ ab\ a7\ 02$

The coordinates of the point Q_{PW} are:

$X = 0xa8b54a6339b296f5c5227670fb1482010b4b07e3642974b40c58a5f1da33370e$
 $fed546eb17c6a707f3fc69671deba10a6de03a55f859473e9074a89b4a7b5488$
 $Y = 0xfebf437ecf21536328b32f4c8e0430d5c0c096001c08a378ac30b8634412f44c$
 $5ba9b709642f51cc3a018cd1599c849cd62917a370eca3bbc6bed5eedabdd77$

During the calculation of the message u_1 on the subject A the parameter alpha, the point $\alpha * P$ and the message u_1 take the following values:

$\alpha = 0x3ce54325db52fe798824aead11bb16fa766857d04a4af7d468672f16d90e7396$

$046a46f815693e85b1ce5464da9270181f82333b0715057bbe8d61d400505f0e$

$\alpha * P$:

$X = 0xb93093eb0fcc463239b7df276e09e592fcfc9b635504ea4531655d76a0a3078e$
 $2b4e51cfe2fa400cc5de9fbe369db204b3e8ed7edd85ee5cca654c1aed70e396$

$Y = 0x809770b8d910ea30bd2fa89736e91dc31815d2d9b31128077eedc371e9f69466$
 $f497dc64dd5b1fad587f860ee256109138c4a9cd96b628e65a8f590520fc882$

u_1 :

$X = 0xe8732d5471901b3eb9a31aaebeac7a6155c2c8fc1c960cb475e14074987dd2c8$
 $4eccafac0835735a5c2df3d1c8dacf4a1d2e38e1e4419f5df4e25b7f8dd90b50$

$Y = 0xd680a41eaec979d49f4752008e9e92eb0efc1950d74b85e852be47f3958d5500$
 $0442d859e5b459de5dc7acaa0c36383cd1f98f271333c6083dcecaf07ac825b8$

During processing a message u_1 , calculation the K_B key and the message u_2 on the subject B the parameters betta, src, $K_B = \text{HASH}(\text{src})$, $\beta * P$ and u_2 take the following values:

$\beta = 0xb5c286a79aa8e97ec0e19bc1959a1d15f12f8c97870ba9d68cc12811a56a3bb1$
 $1440610825796a49d468cdc9c2d02d76598a27973d5960c5f50bce28d8d345f4$

src :

84	59	c2	0c	b5	c5	32	41	6d	b9	28	eb	50	c0	52	0f
b2	1b	9c	d3	9a	4e	76	06	b2	21	be	15	ca	1d	02	da
08	15	de	c4	49	79	c0	8c	7d	23	07	af	24	7d	da	1f
89	ec	81	20	69	f5	d9	cd	e3	06	af	f0	bc	3f	d2	6e
d2	01	b9	53	52	a2	56	06	b6	43	e8	88	30	2e	fc	8d
3e	95	1e	3e	b4	68	4a	db	5c	05	7b	8f	8c	89	b6	cc
0d	ee	d1	00	06	5b	51	8a	1c	71	7f	76	82	ff	61	2b
bc	79	8e	c7	b2	49	0f	b7	00	3f	94	33	87	37	1c	1d

K_B :

53	24	de	f8	48	b6	63	cc	26	42	2f	5e	45	ee	c3	4c
51	d2	43	61	b1	65	60	ca	58	a3	d3	28	45	86	cb	7a

$\beta * P$:

$X = 0x238b38644e440452a99fa6b93d9fd7da0cb83c32d3c1e3cf5c3eb0f9db91$

$e588daedc849ea2fb867ae855a21b4077353c0794716a6480995113d8c20c7af$

$Y = 0xb2273d5734c1897f8d15a7008b862938c8c74ca7e877423d95243eb7ebd02fd2$
 $c456cf9fc956f078a59aa86f19dd1075e5167e4ed35208718ea93161c530ed14$

u_2 :

$X = 0x1830804bf1fb07ebd43f27d03ff71ad9c7c31becaf1d3585dfb9e356c36638dc$
 $d82aba559dec06d46c862566653dfe0b116eb1a68439b0283f4d79ce48408eee$

$Y = 0x23b33ae97fba92e06095c41525aeadf7b5d96fe9ca8e0244ed6c8a565d542d05e$
 $d3044caf8a18ac9a570c5133ba846d61da77f54da2daf13b0def7d90a0796f06$

During processing a message u_2 and calculation the key on the subject A the K_A key takes the following value:

K_A :

53	24	de	f8	48	b6	63	cc	26	42	2f	5e	45	ee	c3	4c
51	d2	43	61	b1	65	60	ca	58	a3	d3	28	45	86	cb	7a

The message $\text{MAC}_A = \text{HMAC}(K_A, 0x01 || \text{ID}_A || \text{ind} || \text{salt} || u_1 || u_2)$ from the subject A takes the following value:

MAC_A:

```
37 e6 1a 43 2d 85 75 9b 30 13 a2 9d d6 82 f1 4d
33 ca 86 89 37 db 4b f2 02 91 ed cf 6b e2 4b 4e
```

The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2) from the subject B takes the following value:

MAC_B:

```
72 dc de 19 5f 26 4b b8 a8 1d 2a fe 2f d9 da 2d
60 12 81 9c 15 f7 11 db 2b c4 c5 74 85 9e 05 3e
```

A.2.5 Curveid-tc26-gost-3410-2012-512-paramSetB

The input protocol parameters in this example take the following values:

N= 3

ind= 1

ID_A:

```
00 00 00 00
```

ID_B:

```
00 00 00 00
```

PW:

```
31 32 33 34 35 36 ('123456')
```

salt:

```
29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
```

Q_ind:

```
X= 0x488cf12b403e539fde9ee32fc36b6ed52aad9ec34ff478c259159a85e99d3dda
dfd5d73606ece351e0f780a14c3e9f14e985d9d7ddec93b064fc89b0c843650
```

```
Y= 0x7bc73c032edc5f2c74dd7d9da12e1856a061ce344a77253f620592752b1f3a3d
ccbc87eb27ec4ed5e236dfb03f3972404747e277671e53a9e412e82aaaf6c3f7
```

The function F (PW, salt, 2000) takes the following values:

F(PW,salt,2000):

```
bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67
```

```
1c 62 13 e3 93 0e fd da 26 45 17 92 c6 20 81 22
```

```
ee 60 d2 00 52 0d 69 5d fd 9f 5f 0f d5 ab a7 02
```

The coordinates of the point Q_PW are:

```
X= 0x2383039092052ed0e8ca3f751c11ebb891b8f32f7c66a437dec86345c63efc4b
alecd04dfc11826dd581cbc1d744754e284c00b04eef9cd6eff22c12432c46fd
```

```
Y= 0x374202580afbaf2f68da8a5c03ab82e71eb4c1f1fdd881aa2911d0206d470039
275d298d5477901565ab826ec4492f67eebcf3194442f272fd2cad9a5f04234f
```

During the calculation of the message u_1 on the subject A the parameter alpha, the point alpha*P and the message u_1 take the following values:

```
alpha=0x715e893fa639bf341296e0623e6d29dadf26b163c278767a7982a989462a3863
fe12aef8bd403d59c4dc4720570d4163db0805c7c10c4e818f9cb785b04b9997
```

alphaP:

```
X= 0x10c479ea1c04d3c2c02b0576a9c42d96226ff033c1191436777f66916030d87d
02fb93738ed7669d07619ffce7c1f3c4db5e5df49e2186d6fa1e2eb5767602b9
```

```
Y= 0x039f6044191404e707f26d59d979136a831cce43e1c5f0600d1ddf8f39d0ca3d
52fdbd943bf04ddced1aa2ce8f5ebd7487acdef239c07d015084d796784f35436
```

u_1:

```
X= 0x0ab9e56fc0d48e4982ee0a0b09507a63dc530181611d9f00d0464724415757b9
```

de1c647178783a0fb4648dfd8e3da1efeb4db29de4711c8599191054ca7de6c4

$\text{Y} = \text{0x4decae941f8d19c44daae9eb132019e116478124e76430b8bee16ce6910a06c8}$
 $\quad \quad \quad \text{a2fed68f4907e4ba17c4f4e3356dc3b3b8647165b9claae54b1c13239bfa8213}$

During processing a message u_1 , calculation the K_B key and the message u_2 on the subject B the parameters betta, src, $K_B = \text{HASH}(\text{src})$, betta^*P and u_2 take the following values:

$\text{betta} = \text{0x30fa8c2b4146c2dbbe82bed04d7378877e8c06753bd0a0ff71ebf2bef8da8f3}$
 $\quad \quad \quad \text{dc0836468e2ce7c5c961281b6505140f8407413f03c2cb1d201ea1286ce30e6d}$

$\text{src}:$

3f	04	02	e4	0a	9d	59	63	20	5b	cd	f4	fd	89	77	91
9b	ba	f4	80	f8	e4	fb	d1	25	5a	ec	e6	ed	57	26	4b
d0	a2	87	98	4f	59	d1	02	04	b5	f4	5e	4d	77	f3	cf
8a	63	b3	1b	eb	2d	f5	9f	8a	f7	3c	20	9c	ca	8b	50
b4	18	d8	01	e4	90	ae	13	3f	04	f4	f3	f4	d8	fe	8e
19	64	6a	1b	af	44	d2	36	fc	c2	1b	7f	4d	8f	c6	a1
e2	9d	6b	69	ac	ce	ed	4e	62	ab	b2	0d	ad	78	ac	f4
fe	b0	ed	83	8e	d9	1e	92	12	ab	a3	89	71	4e	56	0c

$K_B:$

d5	90	e0	5e	f5	ae	ce	8b	7c	fb	fc	71	be	45	5f	29
a5	cc	66	6f	85	cd	b1	7e	7c	c7	16	c5	9f	f1	70	e9

$\text{betta}^*P:$

$\text{X} = \text{0x34c0149e7bb91ae377b02573fcc48af7bfb7b16deb8f9ce870f384688e3241a3}$
 $\quad \quad \quad \text{a868588cc0ef4364cca67d17e3260cd82485c202adc76f895d5df673b1788e67}$

$\text{Y} = \text{0x608e944929bd643569ed5189db871453f13333a1eaf82b2fe1be8100e775f13d}$
 $\quad \quad \quad \text{d9925bd317b63bfaf05024d4a738852332b64501195c1b2ef789e34f23ddafc5}$

$u_2:$

X=	0x66defd2a42f0efe38ed3d4a4dfbed6b86d40f4adf156c86fee1605dbf6b057b1	2fe82a0be4823f7f215b5110673e02e3bf44f0ae26630005fcfd9f01473127eb
Y=	0x36168c6d20c9514556ab442bf63ded0115346916ef45af7e5517f59205d1cc52	ae2e72c3036f13cab7de12932e4a3acd0789f5e2474ff722b81334676c8a3371

During processing a message u_2 and calculation the key on the subject A the K_A key takes the following value:

$K_A:$

d5	90	e0	5e	f5	ae	ce	8b	7c	fb	fc	71	be	45	5f	29
a5	cc	66	6f	85	cd	b1	7e	7c	c7	16	c5	9f	f1	70	e9

The message $\text{MAC}_A = \text{HMAC}(K_A, \text{0x01} \parallel \text{ID}_A \parallel \text{ind} \parallel \text{salt} \parallel u_1 \parallel u_2)$ from the subject A takes the following value:

$\text{MAC}_A:$

9e	c1	a8	74	93	b2	87	c9	ca	c3	da	c2	a2	d7	1b	82
8d	c5	97	7c	b0	03	93	42	c1	5a	cd	fb	66	c8	cf	89

The message $\text{MAC}_B = \text{HMAC}(K_B, \text{0x02} \parallel \text{ID}_B \parallel \text{ind} \parallel \text{salt} \parallel u_1 \parallel u_2)$ from the subject B takes the following value:

$\text{MAC}_B:$

a9	b2	f1	9b	d9	c1	fd	0f	0c	ab	fd	09	52	94	c6	e6
3c	d5	9f	12	cf	8e	fd	01	12	46	0d	b7	aa	20	bb	6e

A.2.6 Curveid-tc26-gost-3410-2012-256-paramSetA

The input protocol parameters in this example take the following values:

```

N= 3
ind= 1
ID_A:
 00 00 00 00
ID_B:
 00 00 00 00
PW:
 31 32 33 34 35 36 ('123456')
salt:
 29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
Q_ind:
 X= 0x5161b08a973d521bdde0cbd45b68aa0470e1058dd936e5bd618fd3373770eed9
 Y= 0xc1633db551677c62b9c2b69d47e503c0f8ca83b6b3109dece0a5f985d77a83a7
The function F (PW, salt, 2000) takes the following values:
F(PW,salt,2000):
 bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
 d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67
 1c 62 13 e3 93 0e fd da 26 45 17 92 c6 20 81 22
 ee 60 d2 00 52 0d 69 5d fd 9f 5f 0f d5 ab a7 02
The coordinates of the point Q_PW are:
X= 0xa0fd0bcfaa07f640c802aa95f42e80b28bb758fbcb7ee2aca2cc0a615b567207
Y= 0x52cf0c960f362894bd097d198999e965bd940c7828e0d2ad38a0097f68135047
During the calculation of the message u_1 on the subject A the parameter
alpha, the point alpha*P and the message u_1 take the following values:
alpha=0x147b72f6684fb8fd1b418a899f7dbeacf5fce60b13685baa95328654a7f0707f
alphaP:
 X= 0x33fbac14eae538275a769417829c431bd9fa622b6f02427ef55bd60ee6bc2888
 Y= 0x22f2ebcf960a82e6cdb4042d3ddda511b2fba925383c2273d952ea2d406eae46
u_1:
 X= 0x8e8929226c7f679ea8c2dfb833d1f8062d62a9672493df02ad7462014c0edbc6
 Y= 0x20f2382c2425aaa638f61e8b70fcf70dae6bcb2f9f341b33ae577c62395aa816
During processing a message u_1, calculation the K_B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH (src), betta*P
and u_2 take the following values:
betta=0x30d5cfadaa0e31b405e6734c03ec4c5df0f02f4ba25c9a3b320ee6453567b4cb
src:
 a3 39 a0 b8 9c ef 1a 6f fd 4c a1 28 04 9e 06 84
 df 4a 97 75 b6 89 a3 37 84 1b f7 d7 91 20 7f 35
 11 86 28 f7 28 8e aa 0f 7e c8 1d a2 0a 24 ff 1e
 69 93 c6 3d 9d d2 6a 90 b7 4d d1 a2 66 28 06 63
K_B:
 7d f7 1a c3 27 ed 51 7d 0d e4 03 e8 17 c6 20 4b
 c1 91 65 b9 d1 00 2b 9f 10 88 a6 cd a6 ea cf 27
betta*P:
 X= 0x2b2d89fab735433970564f2f28cf1b57d640cb902bc6334a538f44155022cb2
 Y= 0x10ef6a82eef1e70f942aa81d6b4ce5dec0ddb9447512962874870e6f2849a96f
u_2:
 X= 0x47182ed8f018fa93a5d837e52724af6051c168ef15e4a40fe926473bc3f1032a

```

$Y = 0x97f3e1e674da53b0ec3ebb1a62a25c7424f4334950daec4d33045f78d9faeeb4$
 During processing a message u_2 and calculation the key on the subject A
 the K_A key takes the following value:

K_A :

```
7d f7 1a c3 27 ed 51 7d 0d e4 03 e8 17 c6 20 4b
c1 91 65 b9 d1 00 2b 9f 10 88 a6 cd a6 ea cf 27
```

The message $MAC_A = \text{HMAC}(K_A, 0x01 || ID_A || \text{ind} || \text{salt} || u_1 || u_2)$
 from the subject A takes the following value:

MAC_A :

```
f5 69 f6 e7 68 9e f0 ba 08 46 98 cc 0e bc ac 59
67 8c 93 26 af 21 f5 4d 3e 90 05 29 32 6b 41 ee
```

The message $MAC_B = \text{HMAC}(K_B, 0x02 || ID_B || \text{ind} || \text{salt} || u_1 || u_2)$
 from the subject B takes the following value:

MAC_B :

```
80 d5 f0 3b 48 22 37 76 43 b4 ff 92 05 dd ed b1
9f 22 80 1f b4 de 0b fb e0 74 55 c2 54 32 45 1e
```

A.2.7 Curveid-tc26-gost-3410-2012-512-paramSetC

The input protocol parameters in this example take the following values:

$N = 3$

$\text{ind} = 1$

ID_A :

```
00 00 00 00
```

ID_B :

```
00 00 00 00
```

PW :

```
31 32 33 34 35 36 ('123456')
```

salt :

```
29 23 be 84 e1 6c d6 ae 52 90 49 f1 f1 bb e9 eb
```

Q_{ind} :

```
X = 0x5b065ead2e94de0ee2e462de204c93c6b2bf3498ad920393cb60259e1a8ffc7c
7e7d4defa20ff4282abf70207e4611d532f40db6800e29d2b53f6ac0713e5b38
```

```
Y = 0xa39a28c59ff7f796b85223b8834384907c626086415487288ed1182ca4487dc1
ae5f37af90fd267b7c0dc8542ea52cd984af54731bc84271d6186d973c91359b
```

The function $F(PW, salt, 2000)$ takes the following values:

$F(PW, salt, 2000)$:

```
bd 04 67 3f 71 49 b1 8e 98 15 5b d1 e2 72 4e 71
d0 09 9a a2 51 74 f7 92 d3 32 6c 6f 18 12 70 67
1c 62 13 e3 93 0e fd da 26 45 17 92 c6 20 81 22
ee 60 d2 00 52 0d 69 5d fd 9f 5f 0f d5 ab a7 02
```

The coordinates of the point Q_{PW} are:

```
X = 0x463e9d38239ddac18e7cc7f6caa7244ae5c49d58dcfd6a56510d7779496744d
75e3e0d5795d4e603f7baea8d24ada989d4179e1db33d1912602fc59470192df
```

```
Y = 0x088874b12c160930aa840f046ee75fa86206f19ca5f431d81e2381d6d947b7b0
30577e40f09b1c16f8e6ef84daddba028f8b6e397a27ece0e13197662659af4d
```

During the calculation of the message u_1 on the subject A the parameter
 α , the point $\alpha * P$ and the message u_1 take the following values:
 $\alpha = 0x0b3fe942126aefc0287f82c6290505aeb117aa8dc033cee56222dd1b9f9e1e5$

377583ba300211ec2c399546b4f54578ee925c238d52530c159c7034ccfa0ddd
alphaP:
X= 0x61427a12468974b5829de1263d91fdfd8e26ea337c6c223595e05b4da4f8fe93
2b532f33c0f4631729422c04f7018a7bf619c026ef0edc4ba2a96b79397eba92
Y= 0x6833806e26791ef1dd01e60c10cc247173b97d7d8d7fea53de4a8a6a444bacc7
042bf35394aef4cfde0f236788f2e9fca9e10f7d7fee54fff951ae17996808c1
u_1:
X= 0x03664ef83e51beaec1f11711f8742b180001c7734a715e4a693758acd9851b38
c6d7e0a316d809b75694ae1b356951a93c91a9b85aa3e3a561742211fd238852
Y= 0x2b92fa93fab060fa86c3039eb2904bc18cbe45032dc3c93ce1c6ba1542a29e0d
790a5f7b63928ed9e50d1fefd6bd00ade4eb021bc62a560567a3419e74dfc08a
During processing a message u_1, calculation the K_B key and the message
u_2 on the subject B the parameters betta, src, K_B = HASH (src), betta * P
and u_2 take the following values:
betta=0xd494d54fb777781d1324ed6088bb0d9d86b8b0a252aa6a3ee70af8ef44b87a6
4cea3a432b61a699bad2d9760d700c2891b6285be0b0bb90f16a40a9b2e0e36a
src:
c2 a3 1a 15 08 52 8a fb 70 be d5 7a 3a 97 9a 3a
8c ed 00 2f 1b 05 8f 99 cb ee 64 56 5c cb ae 42
c5 80 b1 39 18 04 b3 e3 34 d0 2f 70 55 18 ef 16
b7 cf 0e 79 91 76 6f 7e 22 81 f2 87 b1 df cd 34
5c 56 04 ef 1d 9a 8e b8 27 3f 2e 7a 3b fb a4 13
ad 7f 19 59 99 41 f8 f6 73 63 2b e1 43 b1 65 7f
d3 3a 3a de 7d 9f 71 6c e4 0c b5 9e 9d dd a5 0d
db 87 66 57 e7 37 8f f1 55 94 fc 7a 9e 4b 03 48
K_B:
84 14 e1 12 6c 56 a1 1e 1f 5e a0 b7 c3 bd ab e9
8b 26 8b 59 d4 08 f9 7c d0 ea d7 c2 7e e4 9c 15
betta * P:
X= 0xe247677c90ac3c74952c70da0d43f25ece4ac22eda732f7ddd772de7c3e69b22
f7679cc01cae009e442c630c7aa9403a9f11e0fb62cf7af84e77b95210a17edd
Y= 0x63be6dc920e57cb1c5b63fd8b623db6c934b87e0b14468de32c9387515cf3d35
618e945a986424708ef0515ccaa30061ac6870ab56c29c43340736a6c6179c2e
u_2:
X= 0x32260df3ddeabaa9c5c1f55248e8e9a3552cef81a19f0acle10f3b7280a844c
5362b527da1c6ec7eeace2a77aa1167f5e18a4bb6bc6445b4f479ca239245002
Y= 0x04e0612a0c8cd4323535899d0698dd09bb9fc4302016f1b236c86692358ffd98
1cd082c0129763bd4749ee5bb014255d1de0fd7775deccb564213ebc7100001d
During processing a message u_2 and calculation the key on the subject A
the K_A key takes the following value:
K_A:
84 14 e1 12 6c 56 a1 1e 1f 5e a0 b7 c3 bd ab e9
8b 26 8b 59 d4 08 f9 7c d0 ea d7 c2 7e e4 9c 15
The message MAC_A=HMAC (K_A, 0x01 || ID_A || ind || salt || u_1 || u_2)
from the subject A takes the following value:
MAC_A:
53 0b 77 63 c5 9e 7c 98 52 59 ad eb af a4 16 41
c6 f4 35 47 85 01 bd c9 7e a9 cf 88 a6 9a 12 8c

The message MAC_B=HMAC (K_B, 0x02 || ID_B || ind || salt || u_1 || u_2) from the subject B takes the following value:

MAC_B:

```
3f 48 65 b8 8c 81 e5 ac 56 1e 31 c1 b3 d1 d9 0c  
57 e1 e7 4b ac 77 b1 63 ac 60 74 82 4e 99 d3 cc
```

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