

Network Working Group  
Internet-Draft  
Intended status: Informational  
Expires: February 8, 2016

S. Smyshlyaev, Ed.  
E. Alekseev  
I. Oshkin  
V. Popov  
S. Leontiev  
CRYPTO-PRO  
V. Podobaev  
FACTOR-TS  
D. Belyavsky  
TCI  
August 7, 2015

Guidelines on the cryptographic algorithms, accompanying the usage of  
standards GOST R 34.10-2012 and GOST R 34.11-2012  
draft-smyshlyaev-gost-usage-08

## Abstract

The purpose of this document is to make the specifications of the cryptographic algorithms defined by GOST R 34.10-2012 and GOST R 34.11-2012 standards available to the Internet community for their implementation in the cryptographic protocols based on the accompanying algorithms.

These specifications define the pseudorandom functions, the key agreement algorithm based on Diffie-Hellman algorithm, the parameters of elliptic curves, the key derivation functions and the key export functions.

## Status of This Memo

This Internet-Draft is submitted in full conformance with the provisions of BCP 78 and BCP 79.

Internet-Drafts are working documents of the Internet Engineering Task Force (IETF). Note that other groups may also distribute working documents as Internet-Drafts. The list of current Internet-Drafts is at <http://datatracker.ietf.org/drafts/current/>.

Internet-Drafts are draft documents valid for a maximum of six months and may be updated, replaced, or obsoleted by other documents at any time. It is inappropriate to use Internet-Drafts as reference material or to cite them other than as "work in progress."

This Internet-Draft will expire on February 8, 2016.

## Copyright Notice

Copyright (c) 2015 IETF Trust and the persons identified as the document authors. All rights reserved.

This document is subject to BCP 78 and the IETF Trust's Legal Provisions Relating to IETF Documents (<http://trustee.ietf.org/license-info>) in effect on the date of publication of this document. Please review these documents carefully, as they describe your rights and restrictions with respect to this document. Code Components extracted from this document must include Simplified BSD License text as described in Section 4.e of the Trust Legal Provisions and are provided without warranty as described in the Simplified BSD License.

## Table of Contents

1.	Introduction . . . . .	2
2.	Scope . . . . .	3
3.	Conventions used in This Document . . . . .	3
3.1.	Notation . . . . .	3
3.2.	Basic terms and definitions . . . . .	4
4.	Algorithm descriptions . . . . .	6
4.1.	HMAC functions . . . . .	6
4.2.	PRF . . . . .	7
4.3.	VKO algorithms for key agreement . . . . .	8
4.4.	Key derivation function KDF_GOSTR3411_2012_256 . . . . .	10
4.5.	Key derivation function KDF_TREE_GOSTR3411_2012_256 . . . . .	10
4.6.	Key wrap and unwrap . . . . .	11
5.	The parameters of elliptic curves . . . . .	12
5.1.	Canonical form . . . . .	13
5.2.	Twisted Edwards form . . . . .	14
6.	Acknowledgments . . . . .	16
7.	References . . . . .	16
7.1.	Normative References . . . . .	16
7.2.	Informative References . . . . .	17
Appendix A.	Values of the parameter sets . . . . .	18
A.1.	Canonical form parameters . . . . .	18
A.2.	Twisted Edwards form parameters . . . . .	19
Appendix B.	Test examples . . . . .	22
Authors' Addresses	. . . . .	33

## 1. Introduction

The accompanying algorithms are intended for the cryptographic protocols implementation. This memo contains a description of the accompanying algorithms based on Russian national standards GOST R 34.10-2012 [GOST3410-2012] and GOST R 34.11-2012 [GOST3411-2012].

English versions of these standards can be found in [RFC7091] and [RFC6986].

The specifications of algorithms and parameters proposed in this memo are provided on the basis of experience in the development of the cryptographic protocols, as described in the [RFC4357], [RFC4490] and [RFC4491].

This memo contains a description of the accompanying algorithms defining the pseudorandom functions, the key agreement algorithm based on Diffie-Hellman algorithm, the parameters of elliptic curves, the key derivation functions and the key export functions.

The main reason for the development of this document is the need to ensure compatibility of the cryptographic protocol implementation based on the Russian cryptographic standards GOST R 34.10-2012 [GOST3410-2012] and GOST R 34.11-2012 [GOST3411-2012].

## 2. Scope

This memo describes the usage of the digital signature algorithm GOST R 34.10-2012 [GOST3410-2012] and hash function GOST R 34.11-2012 [GOST3411-2012] for encryption and protection the authenticity of the data in public and corporate networks.

## 3. Conventions used in This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC2119].

### 3.1. Notation

This document uses the following notation for the sets and operations on the elements of these sets in accordance with GOST R 34.11-2012 [GOST3411-2012]:

(xor) exclusive-or of two binary vectors of the same length;

$V_n$  the finite-dimensional vector space over  $GF(2)$  of dimension  $n$  with the (xor) operation, for  $n = 0$  the  $V_0$  space consists of a single empty element of size 0;

$U$  the element of  $V_n$ ; in the binary representation  $U = (u_{(n-1)}, u_{(n-2)}, \dots, u_1, u_0)$ , where  $u_i$  in  $\{0, 1\}$ ;

$A|B$  concatenation of vectors  $A$ ,  $B$ , i.e., if  $A$  in  $V_{n1}$ ,  $B$  in  $V_{n2}$ ,  $A = (a_{(n1-1)}, a_{(n1-2)}, \dots, a_0)$ , and  $B = (b_{(n2-1)},$

$b_{(n2-2)}, \dots, b_0$ ), then  $A|B = (a_{(n1-1)}, a_{(n1-2)}, \dots, a_0, b_{(n2-1)}, b_{(n2-2)}, \dots, b_0)$  is an element of  $V_{(n1+n2)}$ ;

$V_{(8, r)}$  the set of byte strings of size  $r$ ; if  $W$  is an element of  $V_{(8, r)}$ , then  $W = (w^0, w^1, \dots, w^{(r-1)})$ , where  $w^0, w^1, \dots, w^{(r-1)}$  are elements of  $V_8$ ; if  $A$  in  $V_{(8, r1)}$ ,  $B$  in  $V_{(8, r2)}$ ,  $A = (a^0, a^1, \dots, a^{(r1-1)})$ , and  $B = (b^0, b^1, \dots, b^{(r2-1)})$ , then  $A|B = (a^0, a^1, \dots, a^{(r1-1)}, b^0, b^1, \dots, b^{(r2-1)})$  is an element of  $V_{(8, r1+r2)}$ ;

Bit representation the bit representation of the element  $W = (w^0, w^1, \dots, w^{(r-1)})$  of  $V_{(8, r)}$ , where  $w^0 = (w_7, w_6, \dots, w_0)$ ,  $w^1 = (w_{15}, w_{14}, \dots, w_8)$ ,  $\dots$ ,  $w^{(r-1)} = (w_{(8r-1)}, w_{(8r-2)}, \dots, w_{(8r-8)})$  are elements of  $V_8$ , is an element  $(w_{(8r-1)}, w_{(8r-2)}, \dots, w_1, w_0)$  of  $V_{(8*r)}$ ;

Byte representation if  $n$  is a multiple of 8,  $r = n/8$ , then the byte representation of the element  $W = (w_{(n-1)}, w_{(n-2)}, \dots, w_0)$  of  $V_n$  is a byte string  $(w^0, w^1, \dots, w^{(r-1)})$  of  $V_{(8, r)}$ , where  $w^0 = (w_7, w_6, \dots, w_0)$ ,  $w^1 = (w_{15}, w_{14}, \dots, w_8)$ ,  $\dots$ ,  $w^{(r-1)} = (w_{(8r-1)}, w_{(8r-2)}, \dots, w_{(8r-8)})$  are elements of  $V_8$ ;

$K$  (key) arbitrary element of  $V_n$ ; if  $K$  in  $V_n$ , then its size (in bits) is equal to  $n$ , where  $n$  can be an arbitrary natural number.

Note: It is proposed to interpret and edit the formulas in accordance with the above definitions.

### 3.2. Basic terms and definitions

This memo uses the following terms, abbreviations and symbols:

Symbols	Meaning
H_256	GOST R 34.11-2012 hash function, 256-bit
H_512	GOST R 34.11-2012 hash function, 512-bit
HMAC	a function for calculating a message authentication code, based on hash function in accordance with [RFC2104]
HMAC_256	an HMAC function based on the hash function H_256, intended for computing a message authentication code
HMAC_512	an HMAC function based on the hash function H_512, intended for computing a message authentication code
PRF	a pseudorandom function, i.e., a transformation that allows to generate pseudorandom sequence of bytes
KDF	a key derivation function, i.e., a transformation, that allows to derive keys and keying material for the root key and random data using a pseudorandom function

To produce a byte sequence of the size  $r$  with functions that give a longer output the output is truncated to the first  $r$  bytes. This remark applies to the following functions:

- o the functions described in Section 4.2;
- o KDF\_TREE\_GOSTR3411\_2012\_256.

When  $n$  is multiple of 8, an element of  $V_n$  can be represented both in the bit and byte form. The result of operation  $\ll|\gg$ , applied to the elements in the bit representation is described in the bit representation. The result of the operation  $\ll|\gg$ , applied to the same elements in byte representation has the byte representation. Thus, the symbol  $\ll|\gg$  is used to refer to two different operations, depending on the form of their arguments. The operation is uniquely determined by the representation of arguments.

Hereinafter all data (the elements of  $V_n$ ) are considered given in the byte representation unless otherwise specified. Operation  $\ll|\gg$  on the arguments of functions, unless explicitly stated, is performed on their byte representation.

If the function is defined outside this document (eg, H\_256) and its definition requires arguments in bit representation, it is assumed that the bit representation of the argument is formed immediately before the calculation of the function (in particular, immediately after the application of the operation <<|>> to the byte representation of the arguments).

If the output of another function that is defined outside of this document is used as the argument of the function defined below and has output value in bit representation, it is assumed that the output value will be translated into the byte representation before substitution in arguments.

#### 4. Algorithm descriptions

For the algorithms described in this paper the possible values of the functions are limited by the permissibility of applying them as the input parameter of the transformations and are assigned by the protocols.

##### 4.1. HMAC functions

This section defines the HMAC transformations based on GOST R 34.11-2012 [GOST3411-2012] algorithms.

###### 4.1.1. HMAC\_GOSTR3411\_2012\_256

This HMAC transformation is based on GOST R 34.11-2012 [GOST3411-2012] algorithm, 256-bit output. The identifier of this transformation is shown below:

```
id-tc26-hmac-gost-3411-12-256 ::= {iso(1) member-body(2) ru(643)
rosstandart(7) tc26(1) algorithms(1) mac(4) hmac-gost-
3411-12-256(1)}.
```

This algorithm uses H\_256 as a hash function for HMAC, described in [RFC2104]. The method of forming the values of ipad and opad is also specified in [RFC2104]. The size of the HMAC\_256 output in bytes is equal to 32, the block size of the iterative procedure for the H\_256 compression function in bytes is equal to 64 (in the notation of [RFC2104], L = 32 and B = 64, respectively).

###### 4.1.2. HMAC\_GOSTR3411\_2012\_512

This HMAC transformation is based on GOST R 34.11-2012 [GOST3411-2012] algorithm, 512-bit output. The identifier of this transformation is shown below:

```
id-tc26-hmac-gost-3411-12-512 ::= {iso(1) member-body(2) ru(643)
rosstandart(7) tc26(1) algorithms(1) mac(4) hmac-gost-
3411-12-512(2)}.
```

This algorithm uses H\_512 as a hash function for HMAC, described in [RFC2104]. The method of forming the values of ipad and opad is also specified in [RFC2104]. The size of the HMAC\_512 output in bytes is equal to 64, the block size of the iterative procedure for the H\_512 compression function in bytes is equal to 64 (in the notation of [RFC2104], L = 64 and B = 64, respectively).

## 4.2. PRF

This section defines six HMAC-based PRF transformations recommended for usage. Two of them are designed for the TLS protocol and four are designed for the IPsec protocol.

### 4.2.1. PRFs for the TLS protocol

#### 4.2.1.1. PRF\_TLS\_GOSTR3411\_2012\_256

This is the transformation providing the pseudorandom function of the TLS protocol (versions 1.0, 1.1, 1.2) in accordance with GOST R 34.11-2012 [GOST3411-2012]; the transformation uses P\_GOSTR3411\_2012\_256 function that is similar to the P\_hash function in Section 5 of [RFC2246], where HMAC\_256 function (defined in Section 4.1.1) is used as an HMAC\_hash function.

```
PRF_TLS_GOSTR3411_2012_256 (secret, label, seed) =
= P_GOSTR3411_2012_256 (secret, label | seed).
```

#### 4.2.1.2. PRF\_TLS\_GOSTR3411\_2012\_512

This is the transformation providing the pseudorandom function of the TLS protocol in accordance with GOST R 34.11-2012 [GOST3411-2012]; the transformation uses P\_GOSTR3411\_2012\_512 function that is similar to the P\_hash function in Section 5 of [RFC2246], where HMAC\_512 function (defined in Section 4.1.2) is used as an HMAC\_hash function.

```
PRF_TLS_GOSTR3411_2012_512 (secret, label, seed) =
= P_GOSTR3411_2012_512 (secret, label | seed).
```

### 4.2.2. PRFs for the IPsec protocols based on GOST R 34.11-2012

IPsec family protocols use the pseudorandom functions for the purposes of keying material generation and authentication. The specifications for the version 1 (IKEv1) [RFC2409] and version 2

(IKEv2) [RFC7296] of the Internet Key Exchange protocol contain definitions of using PRF in various parts of the protocols.

#### 4.2.2.1. PRF in the IKEv1 protocol

According to the Section 4 of [RFC2409] if a PRF is not negotiated, the HMAC based on the negotiated hash algorithm is used. So, when GOST R 34.11-2012 [GOST3411-2012] is used as a hash function in IKEv1, HMAC\_GOST3411\_2012\_512 is used as a PRF depending on the negotiated hash algorithm.

#### 4.2.2.2. PRF in the IKEv2 protocol

IKEv2 has no default PRF. This document specifies that either HMAC\_GOST3411\_2012\_256 or HMAC\_GOST3411\_2012\_512 must be used as PRF for the IKEv2 protocol.

### 4.3. VKO algorithms for key agreement

This section specifies the key agreement algorithms using GOST R 34.10-2012 [GOST3410-2012].

#### 4.3.1. VKO\_GOSTR3410\_2012\_256

The VKO\_GOSTR3410\_2012\_256 transformation is used for an agreement of the VKO 256-bit keys and is based on GOST R 34.11-2012 [GOST3411-2012], 256-bit. This algorithm can be applied for a key agreement using the GOST R 34.10-2012 [GOST3410-2012] 256-bit and 512-bit keys.

The algorithm is designed to produce an encryption key or a keying material of size 256 bits to be used in various cryptographic protocols. Key or keying material KEK\_VKO (x, y, UKM) is produced from the private key x of one side, the public key  $y^P$  of the opposite side and UKM value, considered as a number.

The algorithm can be used for deriving both static and ephemeral key with the public key size  $n \geq 512$  bits including the case where one side uses a static key and the other - ephemeral.

UKM parameter is optional (the default UKM = 1) and can take any value from 1 to  $2^{(n/2)}-1$ . It is allowed to use a nonzero UKM of arbitrary size not exceeding  $n/2$  bits. If at least one of the parties uses static keys, the recommended length of UKM is 64 bits or more.

K is calculated using formula



$$K(x, y, UKM) = (m/q * UKM * x \bmod q) * (y * P),$$

where  $m$  and  $q$  are the parameters of the elliptic curve defined in the GOST R 34.10-2012 [GOST3410-2012] notation.

KEK\_VKO is calculated using formula

$$KEK\_VKO(x, y, UKM) = H_{256}(K(x, y, UKM)).$$

This algorithm is defined similar to Section 5.2 of [RFC4357], but applies the hash function  $H_{256}$  instead of the hash function GOST R 34.11-94 [GOST3411-94] (referred as `gostR3411`) and  $K(x, y, UKM)$  is calculated with public key size  $n \geq 512$  bits and UKM size up to  $n/2$  bits.

#### 4.3.2. VKO\_GOSTR3410\_2012\_512

The `VKO_GOSTR3410_2012_512` transformation is used for an agreement of the VKO 512-bit keys and is based on GOST R 34.11-2012 [GOST3411-2012], 512-bit. This algorithm can be applied for a key agreement using the GOST R 34.10-2012 [GOST3410-2012] 512-bit keys.

The algorithm is designed to produce an encryption key or keying material of size 512 bits to be used in cryptographic protocols. Key or keying material `KEK_VKO(x, y, UKM)` is produced from the private key  $x$  of one side, the public key  $y * P$  of the opposite side and UKM value, considered as a number.

The algorithm can be used for both static and ephemeral key with the public key size  $n \geq 1024$  bits including the case where one side uses a static key and the other uses an ephemeral one.

UKM parameter is optional (the default  $UKM = 1$ ) and can take any value from 1 to  $2^{(n/2)} - 1$ . It is allowed to use a nonzero UKM of arbitrary size not exceeding  $n/2$  bits. If at least one of the parties uses static keys, the recommended length of UKM is 128 bits or more.

$$K(x, y, UKM) = (m/q * UKM * x \bmod q) * (y * P),$$

where  $m$  and  $q$  - the parameters of the elliptic curve according to GOST R 34.10-2012 [GOST3410-2012] notation.

$$KEK\_VKO(x, y, UKM) = H_{512}(K(x, y, UKM)).$$

This algorithm is defined similar to Section 5.2 of [RFC4357], but instead of the hash function GOST R 34.11-94 [GOST3411-94] (referred as `gostR3411`) applies the hash function  $H_{256}$ , and  $K(x, y, UKM)$  is

calculated at the public key size  $n \geq 1024$  bits and UKM size up to  $n/2$  bits.

#### 4.4. Key derivation function KDF\_GOSTR3411\_2012\_256

The key derivation function KDF\_GOSTR3411\_2012\_256 based on HMAC\_256 function is designed to generate a 256-bit keying material and is given by:

$$\text{KDF}(\text{K\_in}, \text{label}, \text{seed}) = \text{HMAC\_256}(\text{K\_in}, \text{0x01} \mid \text{label} \mid \text{0x00} \mid \text{seed} \mid \text{0x01} \mid \text{0x00}),$$

where

- o K\_in -- derivation key,
- o label, seed -- the parameters, fixed and assigned by a protocol.

The key derivation function KDF\_GOSTR3411\_2012\_256 is a special case of KDF\_TREE\_GOSTR3411\_2012 function, described in the next section.

#### 4.5. Key derivation function KDF\_TREE\_GOSTR3411\_2012\_256

The key derivation function KDF\_TREE\_GOSTR3411\_2012\_256 based on HMAC\_256 and is given by:

$$\text{KDF\_TREE}(\text{K\_in}, \text{label}, \text{seed}, \text{R}) = \text{K}(1) \mid \text{K}(2) \mid \text{K}(3) \mid \text{K}(4) \mid \dots,$$

$$\text{K}(i) = \text{HMAC\_256}(\text{K\_in}, [i]_2 \mid \text{label} \mid \text{0x00} \mid \text{seed} \mid [L]_2), i \geq 1,$$

where

- R a fixed external parameter, with possible values of 1, 2, 3 or 4;
- K\_in derivation key;
- L the required size (in bits) of the generated keying material (an integer, not exceeding  $256 \cdot (2^{(8 \cdot R)} - 1)$ );
- [L]\_2 byte representation of L, in network byte order;
- i iteration counter;
- [i]\_2 byte representation of the iteration counter (in the network byte order), the number of bytes in the representation [i]\_2 is equal to R (no more than 4 bytes);

label, seed the parameters, fixed and assigned by a protocol.

The key derivation function `KDF_TREE_GOSTR3411_2012_256` is intended for generating a keying material in size of  $L$ , not exceeding  $256 \cdot (2^{(8 \cdot R)} - 1)$  bits, and utilizes general principles of the input and output for the key derivation function outlined in Section 5.1 of NIST SP 800-108 [NISTSP800-108]. HMAC\_256 algorithm with 256-bit output described in Section 4.1.1 is selected as a pseudorandom function.

When  $R = 1$  and  $L = 256$  the function `KDF_TREE_GOSTR3411_2012_256` is equivalent to `KDF_GOSTR3411_2012_256` from the previous section.

Each key derived from the keying material formed using the derivation key  $K_{in}$  (0-level key) may be a 1-level diversification key and may be used to generate a new keying material. The keying material derived from the 1-level derivation key can be split down into the 2nd level derivation keys. The application of this procedure leads to the construction of the key tree with the root key and the formation of the keying material to the hierarchy of the levels, as described in Section 6 of NIST SP 800-108 [NISTSP800-108]. The partitioning procedure for keying material at each level is defined according to the specific protocols.

#### 4.6. Key wrap and unwrap

Wrapped representation of the secret key  $K$  (GOST R 34.10-2012 [GOST3410-2012] key or GOST 28147-89 [GOST28147-89] key) is formed as follows by using a given export key  $K_e$  (GOST 28147-89 [GOST28147-89] key) and a random UKM vector from 8 to 16 bytes in size:

1. Generate a random UKM vector.
2. With the key derivation function, using export key  $K_e$  as a derivation key, and a UKM vector as the value of seed, generate a key, denoted by  $KEK_e$  (UKM), where

$$KEK_e \text{ (UKM)} = \text{KDF} (K_e, \text{label}, \text{UKM}),$$

where KDF function (see previous section) is used as a key derivation function for the fixed value

$$\text{label} = (0x26 \mid 0xBD \mid 0xB8 \mid 0x78),$$

and the seed value that is equal to UKM.

3. MAC value GOST 28147-89 (4-byte) for the data  $K$  and the key  $KEK_e$  (UKM) is calculated, initialization vector (IV) in this case is

equal to the first 8 bytes of UKM. The resulting value is denoted as CEK\_MAC.

4. The key K is encrypted by the GOST 28147-89 algorithm in the Electronic Codebook (ECB) mode with the key KEK\_e (UKM). The encoding result is denoted as CEK\_ENC.
5. The wrapped representation of the key is considered (UKM | CEK\_ENC | CEK\_MAC).

During the key import the value of key K is restored as follows from the wrapped representation of the key (GOST R 34.10-2012 [GOST3410-2012] key or GOST 28147-89 key [GOST28147-89] key) and the export key K\_e:

1. From the wrapped representation of the key selects the sets UKM, CEK\_ENC, and CEK\_MAC.
2. With the key derivation function, using the export key K\_e as a derivation key, and a random UKM value as the value of seed, generates a key, denoted by KEK\_e(UKM), where

$$\text{KEK}_e(\text{UKM}) = \text{KDF}(\text{K}_e, \text{label}, \text{UKM}).$$

3. The CEK\_ENC set is decrypted by the GOST 28147-89 algorithm in the Electronic Codebook (ECB) mode with the key KEK\_e(UKM). The unwrapped key K is assumed to be equal to the result of decryption.
4. MAC value GOST 28147-89 (4-byte) for the data K and the key KEK\_e(UKM) is calculated, initialization vector (IV) in this case is equal to the first 8 bytes of UKM. If the result does not equal to CEK\_MAC, an error is returned.

The algorithms for wrapping and unwrapping of the GOST R 34.10-2012 [GOST3410-2012] keys are modifications of the CryptoPro Key Wrap and CryptoPro Key Unwrap algorithms, described in Sections 6.3 and 6.4 of [RFC4357].

## 5. The parameters of elliptic curves

This section defines the elliptic curves parameters and identifiers that are recommended for the usage with signature and verification algorithms of digital signature in accordance with GOST R 34.10-2012 [GOST3410-2012] standard and with the key agreement algorithms VKO\_GOSTR3410\_2012\_256 and VKO\_GOSTR3410\_2012\_512.

This document does not negate the use of other parameters of the elliptic curves.

## 5.1. Canonical form

This section defines the elliptic curves parameters of the GOST R 34.10-2012 [GOST3410-2012] standard for the case of elliptic curves with a prime 512-bit modulus in canonical (Weierstrass) form, that is given by the following equation defined in GOST R 34.10-2012 [GOST3410-2012]:

$$y^2 = x^3 + ax + b.$$

In case of an elliptic curves with 256-bit the parameters defined in [RFC4357] are proposed to use.

### 5.1.1. Parameters and identifiers

The parameters for each of the elliptic curve are represented by the following values which are defined in GOST R 34.10-2012 [GOST3410-2012]:

- p the elliptic curve modulus;
- a, b the coefficients of the equation of the elliptic curve in the canonical form;
- q the order of the elliptic curve;
- (x, y) the coordinates of a point P (generator of the prime order group) of the elliptic curve in the canonical form.

Both sets of the parameters are presented as ASN structures of the form:

```
SEQUENCE {
  a    INTEGER,
  b    INTEGER,
  p    INTEGER,
  q    INTEGER,
  x    INTEGER,
  y    INTEGER
}
```

The parameter sets have the following identifiers:

1. `id-tc26-gost-3410-12-512-paramSetA := {iso(1) member-body(2) ru(643) rosstandart(7) tc26(1) constants(2) sign-constants(1) gost-3410-12-512-constants(2) paramSetA(1)};`
2. `id-tc26-gost-3410-12-512-paramSetB := {iso(1) member-body(2) ru(643) rosstandart(7) tc26(1) constants(2) sign-constants(1) gost-3410-12-512-constants(2) paramSetB(2)}.`

Corresponding values of the parameter sets can be found in Appendix A.1.

## 5.2. Twisted Edwards form

This section defines the elliptic curves parameters and identifiers of the GOST R 34.10-2012 [GOST3410-2012] standard for the case of elliptic curves that have a representation in Twisted Edwards form with a prime 256-bit and 512-bit modulus.

A Twisted Edwards curve  $E$  over a finite prime field  $F_p$ ,  $p > 3$ , is an elliptic curve defined by the equation:

$$e \cdot u^2 + v^2 = 1 + d \cdot u^2 \cdot v^2,$$

where  $e, d$  are in  $F_p$ ,  $ed(e-d) \neq 0$ .

A Twisted Edwards curve has an equivalent representation in the Weierstrass form defined by parameters  $a, b$ . The parameters  $a, b, e, d$  are related as follows:

$$\begin{aligned} a &= s^2 - 3 \cdot t^2, \\ b &= 2 \cdot t^3 - t \cdot s^2, \end{aligned}$$

where

$$\begin{aligned} s &= (e - d) / 4, \\ t &= (e + d) / 6, \end{aligned}$$

Coordinate transformation is defined as follows:

$$\begin{aligned} (u, v) &\rightarrow (x, y) = (s(1 + v) / (1 - v) + t, s(1 + v) / ((1 - v) \\ &u)), \\ (x, y) &\rightarrow (u, v) = ((x - t) / y, (x - t - s) / (x - t + s)). \end{aligned}$$

### 5.2.1. Parameters and identifiers

The parameters for each of the elliptic curve are represented by the following values which are defined in GOST R 34.10-2012 [GOST3410-2012]:

- p the elliptic curve modulus;
- a, b the coefficients of the equation of the elliptic curve in the canonical form;
- e, d the coefficients of the equation of the elliptic curve in the Twisted Edwards form;
- m the order of the elliptic curve group;
- q the order of the subgroups of prime order elliptic curve group;
- (x, y) the coordinates of a point P (generator of the prime order group) of the elliptic curve in the canonical form;
- (u, v) the coordinates of a point P (generator of the prime order group) of the elliptic curve in the Twisted Edwards form.

Both sets of the parameters are presented as ASN structures of the form:

```

SEQUENCE {
p      INTEGER,
a      INTEGER,
b      INTEGER,
e      INTEGER,
d      INTEGER,
m      INTEGER,
q      INTEGER,
x      INTEGER,
y      INTEGER,
u      INTEGER,
v      INTEGER
}

```

The parameter sets have the following identifiers:

1. id-tc26-gost-3410-2012-256-paramSetA ::= {iso(1) member-body(2) ru(643) rosstandart(7) tc26(1) constants(2) sign-constants(1) gost-3410-12-256-constants(1) paramSetA(1)};
2. id-tc26-gost-3410-2012-512-paramSetC ::= {iso(1) member-body(2) ru(643) rosstandart(7) tc26(1) constants(2) sign-constants(1) gost-3410-12-512-constants(2) paramSetC(3)}.

Corresponding values of the parameter sets can be found in Appendix A.2.

## 6. Acknowledgments

We thank Valery Smyslov, Igor Ustinov, Basil Dolmatov and Russ Housley for their careful readings and useful comments.

## 7. References

### 7.1. Normative References

[GOST28147-89]

Gosudarstvennyi Standard of USSR, Government Committee of the USSR for Standards, "Systems of information processing. Cryptographic data security. Algorithms of cryptographic transformation", GOST 28147-89, 1989.

[GOST3410-2012]

Federal Agency on Technical Regulating and Metrology, "Information technology. Cryptographic data security. Signature and verification processes of [electronic] digital signature", GOST R 34.10-2012, 2012.

[GOST3411-2012]

Federal Agency on Technical Regulating and Metrology, "Information technology. Cryptographic Data Security. Hashing function", GOST R 34.11-2012, 2012.

[GOST3411-94]

Federal Agency on Technical Regulating and Metrology, "Information technology. Cryptographic Data Security. Hashing function", GOST R 34.11-94, 1994.

[RFC2104] Krawczyk, H., Bellare, M., and R. Canetti, "HMAC: Keyed-Hashing for Message Authentication", RFC 2104, DOI 10.17487/RFC2104, February 1997, <<http://www.rfc-editor.org/info/rfc2104>>.

[RFC2119] Bradner, S., "Key words for use in RFCs to Indicate Requirement Levels", BCP 14, RFC 2119, DOI 10.17487/RFC2119, March 1997, <<http://www.rfc-editor.org/info/rfc2119>>.

[RFC2409] Harkins, D. and D. Carrel, "The Internet Key Exchange (IKE)", RFC 2409, DOI 10.17487/RFC2409, November 1998, <<http://www.rfc-editor.org/info/rfc2409>>.



- [RFC4357] Popov, V., Kurepkin, I., and S. Leontiev, "Additional Cryptographic Algorithms for Use with GOST 28147-89, GOST R 34.10-94, GOST R 34.10-2001, and GOST R 34.11-94 Algorithms", RFC 4357, DOI 10.17487/RFC4357, January 2006, <<http://www.rfc-editor.org/info/rfc4357>>.
- [RFC7296] Kaufman, C., Hoffman, P., Nir, Y., Eronen, P., and T. Kivinen, "Internet Key Exchange Protocol Version 2 (IKEv2)", STD 79, RFC 7296, DOI 10.17487/RFC7296, October 2014, <<http://www.rfc-editor.org/info/rfc7296>>.

## 7.2. Informative References

- [NISTSP800-108] National Institute of Standards and Technology, "Recommendation for Key Derivation Using Pseudorandom Functions", NIST SP 800-108, October 2009.
- [RFC2246] Dierks, T. and C. Allen, "The TLS Protocol Version 1.0", RFC 2246, DOI 10.17487/RFC2246, January 1999, <<http://www.rfc-editor.org/info/rfc2246>>.
- [RFC4490] Leontiev, S., Ed. and G. Chudov, Ed., "Using the GOST 28147-89, GOST R 34.11-94, GOST R 34.10-94, and GOST R 34.10-2001 Algorithms with Cryptographic Message Syntax (CMS)", RFC 4490, DOI 10.17487/RFC4490, May 2006, <<http://www.rfc-editor.org/info/rfc4490>>.
- [RFC4491] Leontiev, S., Ed. and D. Shefanovski, Ed., "Using the GOST R 34.10-94, GOST R 34.10-2001, and GOST R 34.11-94 Algorithms with the Internet X.509 Public Key Infrastructure Certificate and CRL Profile", RFC 4491, DOI 10.17487/RFC4491, May 2006, <<http://www.rfc-editor.org/info/rfc4491>>.
- [RFC6986] Dolmatov, V., Ed. and A. Degtyarev, "GOST R 34.11-2012: Hash Function", RFC 6986, DOI 10.17487/RFC6986, August 2013, <<http://www.rfc-editor.org/info/rfc6986>>.
- [RFC7091] Dolmatov, V., Ed. and A. Degtyarev, "GOST R 34.10-2012: Digital Signature Algorithm", RFC 7091, DOI 10.17487/RFC7091, December 2013, <<http://www.rfc-editor.org/info/rfc7091>>.

## Appendix A. Values of the parameter sets

## A.1. Canonical form parameters

Parameter set: id-tc26-gost-3410-12-512-paramSetA

SEQUENCE

{

  OBJECT IDENTIFIER

  id-tc26-gost-3410-12-512-paramSetA

  SEQUENCE

  {

    INTEGER

    00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FD  
     C4

    INTEGER

    00 E8 C2 50 5D ED FC 86 DD C1 BD 0B 2B 66 67 F1  
     DA 34 B8 25 74 76 1C B0 E8 79 BD 08 1C FD 0B 62  
     65 EE 3C B0 90 F3 0D 27 61 4C B4 57 40 10 DA 90  
     DD 86 2E F9 D4 EB EE 47 61 50 31 90 78 5A 71 C7  
     60

    INTEGER

    00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FD  
     C7

    INTEGER

    00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
     FF 27 E6 95 32 F4 8D 89 11 6F F2 2B 8D 4E 05 60  
     60 9B 4B 38 AB FA D2 B8 5D CA CD B1 41 1F 10 B2  
     75

    INTEGER 3

    INTEGER

    00 75 03 CF E8 7A 83 6A E3 A6 1B 88 16 E2 54 50  
     E6 CE 5E 1C 93 AC F1 AB C1 77 80 64 FD CB EF A9  
     21 DF 16 26 BE 4F D0 36 E9 3D 75 E6 A5 0E 3A 41  
     E9 80 28 FE 5F C2 35 F5 B8 89 A5 89 CB 52 15 F2  
     A4

  }

}

Parameter set: id-tc26-gost-3410-12-512-paramSetB

SEQUENCE

{

OBJECT IDENTIFIER

id-tc26-gost-3410-12-512-paramSetB

SEQUENCE

{

INTEGER

00 80 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 6C

INTEGER

00 68 7D 1B 45 9D C8 41 45 7E 3E 06 CF 6F 5E 25  
 17 B9 7C 7D 61 4A F1 38 BC BF 85 DC 80 6C 4B 28  
 9F 3E 96 5D 2D B1 41 6D 21 7F 8B 27 6F AD 1A B6  
 9C 50 F7 8B EE 1F A3 10 6E FB 8C CB C7 C5 14 01  
 16

INTEGER

00 80 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 6F

INTEGER

00 80 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00  
 01 49 A1 EC 14 25 65 A5 45 AC FD B7 7B D9 D4 0C  
 FA 8B 99 67 12 10 1B EA 0E C6 34 6C 54 37 4F 25  
 BD

INTEGER 2

INTEGER

00 1A 8F 7E DA 38 9B 09 4C 2C 07 1E 36 47 A8 94  
 0F 3C 12 3B 69 75 78 C2 13 BE 6D D9 E6 C8 EC 73  
 35 DC B2 28 FD 1E DF 4A 39 15 2C BC AA F8 C0 39  
 88 28 04 10 55 F9 4C EE EC 7E 21 34 07 80 FE 41  
 BD

}

}

A.2. Twisted Edwards form parameters

Parameter set: id-tc26-gost-3410-2012-256-paramSetA

## SEQUENCE

```
{
  OBJECT IDENTIFIER
  id-tc26-gost-3410-2012-256-paramSetA
  SEQUENCE
  {
    INTEGER
    00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF
    FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF
    97
    INTEGER
    00 C2 17 3F 15 13 98 16 73 AF 48 92 C2 30 35 A2
    7C E2 5E 20 13 BF 95 AA 33 B2 2C 65 6F 27 7E 73
    35
    INTEGER
    29 5F 9B AE 74 28 ED 9C CC 20 E7 C3 59 A9 D4 1A
    22 FC CD 91 08 E1 7B F7 BA 93 37 A6 F8 AE 95 13
    INTEGER
    01
    INTEGER
    06 05 F6 B7 C1 83 FA 81 57 8B C3 9C FA D5 18 13
    2B 9D F6 28 97 00 9A F7 E5 22 C3 2D 6D C7 BF FB
    INTEGER
    01 00 00 00 00 00 00 00 00 00 00 00 00 00 00
    00 3F 63 37 7F 21 ED 98 D7 04 56 BD 55 B0 D8 31
    9C
    INTEGER
    40 00 00 00 00 00 00 00 00 00 00 00 00 00 00
    0F D8 CD DF C8 7B 66 35 C1 15 AF 55 6C 36 0C 67
    INTEGER
    00 91 E3 84 43 A5 E8 2C 0D 88 09 23 42 57 12 B2
    BB 65 8B 91 96 93 2E 02 C7 8B 25 82 FE 74 2D AA
    28
    INTEGER
    32 87 94 23 AB 1A 03 75 89 57 86 C4 BB 46 E9 56
    5F DE 0B 53 44 76 67 40 AF 26 8A DB 32 32 2E 5C
    INTEGER
    0D
    INTEGER
    60 CA 1E 32 AA 47 5B 34 84 88 C3 8F AB 07 64 9C
    E7 EF 8D BE 87 F2 2E 81 F9 2B 25 92 DB A3 00 E7
  }
}
```

Parameter set: id-tc26-gost-3410-2012-512-paramSetC

## SEQUENCE

{

OBJECT IDENTIFIER

id-tc26-gost-3410-2012-512-paramSetC

SEQUENCE

{

INTEGER

00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF FF FF FF FF FF FF FF FF FF FF FF FF FF FD  
C7

INTEGER

00 DC 92 03 E5 14 A7 21 87 54 85 A5 29 D2 C7 22  
FB 18 7B C8 98 0E B8 66 64 4D E4 1C 68 E1 43 06  
45 46 E8 61 C0 E2 C9 ED D9 2A DE 71 F4 6F CF 50  
FF 2A D9 7F 95 1F DA 9F 2A 2E B6 54 6F 39 68 9B  
D3

INTEGER

00 B4 C4 EE 28 CE BC 6C 2C 8A C1 29 52 CF 37 F1  
6A C7 EF B6 A9 F6 9F 4B 57 FF DA 2E 4F 0D E5 AD  
E0 38 CB C2 FF F7 19 D2 C1 8D E0 28 4B 8B FE F3  
B5 2B 8C C7 A5 F5 BF 0A 3C 8D 23 19 A5 31 25 57  
E1

INTEGER

01

INTEGER

00 9E 4F 5D 8C 01 7D 8D 9F 13 A5 CF 3C DF 5B FE  
4D AB 40 2D 54 19 8E 31 EB DE 28 A0 62 10 50 43  
9C A6 B3 9E 0A 51 5C 06 B3 04 E2 CE 43 E7 9E 36  
9E 91 A0 CF C2 BC 2A 22 B4 CA 30 2D BB 33 EE 75  
50

INTEGER

00 FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF 26 33 6E 91 94 1A AC 01 30 CE A7 FD 45 1D 40  
B3 23 B6 A7 9E 9D A6 84 9A 51 88 F3 BD 1F C0 8F  
B4

INTEGER

3F FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
FF FF FF FF FF FF FF FF FF FF FF FF FF FF FF  
C9 8C DB A4 65 06 AB 00 4C 33 A9 FF 51 47 50 2C  
C8 ED A9 E7 A7 69 A1 26 94 62 3C EF 47 F0 23 ED

INTEGER

00 E2 E3 1E DF C2 3D E7 BD EB E2 41 CE 59 3E F5  
DE 22 95 B7 A9 CB AE F0 21 D3 85 F7 07 4C EA 04  
3A A2 72 72 A7 AE 60 2B F2 A7 B9 03 3D B9 ED 36  
10 C6 FB 85 48 7E AE 97 AA C5 BC 79 28 C1 95 01

```

48
INTEGER
00 F5 CE 40 D9 5B 5E B8 99 AB BC CF F5 91 1C B8
57 79 39 80 4D 65 27 37 8B 8C 10 8C 3D 20 90 FF
9B E1 8E 2D 33 E3 02 1E D2 EF 32 D8 58 22 42 3B
63 04 F7 26 AA 85 4B AE 07 D0 39 6E 9A 9A DD C4
0F
INTEGER
12
INTEGER
46 9A F7 9D 1F B1 F5 E1 6B 99 59 2B 77 A0 1E 2A
0F DF B0 D0 17 94 36 8D 9A 56 11 7F 7B 38 66 95
22 DD 4B 65 0C F7 89 EE BF 06 8C 5D 13 97 32 F0
90 56 22 C0 4B 2B AA E7 60 03 03 EE 73 00 1A 3D
}
}

```

#### Appendix B. Test examples

##### 1) HMAC\_GOSTR3411\_2012\_256

Key K:

```

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

```

T:

```

01 26 bd b8 78 00 af 21 43 41 45 65 63 78 01 00

```

HMAC\_256(K, T) value:

```

a1 aa 5f 7d e4 02 d7 b3 d3 23 f2 99 1c 8d 45 34
01 31 37 01 0a 83 75 4f d0 af 6d 7c d4 92 2e d9

```

## 2) HMAC\_GOSTR3411\_2012\_512

Key K:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

T:

01 26 bd b8 78 00 af 21 43 41 45 65 63 78 01 00

HMAC\_256(K, T) value:

a5 9b ab 22 ec ae 19 c6 5f bd e6 e5 f4 e9 f5 d8  
54 9d 31 f0 37 f9 df 9b 90 55 00 e1 71 92 3a 77  
3d 5f 15 30 f2 ed 7e 96 4c b2 ee dc 29 e9 ad 2f  
3a fe 93 b2 81 4f 79 f5 00 0f fc 03 66 c2 51 e6

## 3) PRF\_TLS\_GOSTR3411\_2012\_256

Key K:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

Seed:

18 47 1d 62 2d c6 55 c4 d2 d2 26 96 91 ca 4a 56  
0b 50 ab a6 63 55 3a f2 41 f1 ad a8 82 c9 f2 9a

Label:

11 22 33 44 55

Output T1:

ff 09 66 4a 44 74 58 65 94 4f 83 9e bb 48 96 5f  
15 44 ff 1c c8 e8 f1 6f 24 7e e5 f8 a9 eb e9 7f

Output T2:

c4 e3 c7 90 0e 46 ca d3 db 6a 01 64 30 63 04 0e  
c6 7f c0 fd 5c d9 f9 04 65 23 52 37 bd ff 2c 02

4) PRF\_TLS\_GOSTR3411\_2012\_512

Key K:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

Seed:

18 47 1d 62 2d c6 55 c4 d2 d2 26 96 91 ca 4a 56  
0b 50 ab a6 63 55 3a f2 41 f1 ad a8 82 c9 f2 9a

Label:

11 22 33 44 55

Output T1:

f3 51 87 a3 dc 96 55 11 3a 0e 84 d0 6f d7 52 6c  
5f c1 fb de c1 a0 e4 67 3d d6 d7 9d 0b 92 0e 65  
ad 1b c4 7b b0 83 b3 85 1c b7 cd 8e 7e 6a 91 1a  
62 6c f0 2b 29 e9 e4 a5 8e d7 66 a4 49 a7 29 6d

Output T2:

e6 1a 7a 26 c4 d1 ca ee cf d8 0c ca 65 c7 1f 0f  
88 c1 f8 22 c0 e8 c0 ad 94 9d 03 fe e1 39 57 9f  
72 ba 0c 3d 32 c5 f9 54 f1 cc cd 54 08 1f c7 44  
02 78 cb a1 fe 7b 7a 17 a9 86 fd ff 5b d1 5d 1f



## 5) PRF\_IPSEC\_KEYMAT\_GOSTR3411\_2012\_256

Key K:

c9 a9 a7 73 20 e2 cc 55 9e d7 2d ce 6f 47 e2 19  
2c ce a9 5f a6 48 67 05 82 c0 54 c0 ef 36 c2 21

Data of S:

01 26 bd b8 78 00 1d 80 60 3c 85 44 c7 27 01 00

Output T1:

21 01 d8 0c 47 db 54 bc 3c 82 9b 8c 30 7c 47 55  
50 88 83 a6 d6 9e 60 1b f7 aa fb 0a bc a4 ed 95

Output T2:

33 b8 4e d0 8f 93 56 f8 1d f8 d2 79 f0 79 c9 02  
87 cb 45 2c 81 d4 1e 80 38 43 08 86 c1 92 12 aa

## 6) PRF\_IPSEC\_PRFPLUS\_GOSTR3411\_2012\_256

Key K:

c9 a9 a7 73 20 e2 cc 55 9e d7 2d ce 6f 47 e2 19  
2c ce a9 5f a6 48 67 05 82 c0 54 c0 ef 36 c2 21

Data of S:

01 26 bd b8 78 00 1d 80 60 3c 85 44 c7 27 01 00

Output T1:

2d e5 ee 84 e1 3d 7b e5 36 16 67 39 13 37 0a b0  
54 c0 74 b7 9b 69 a8 a8 46 82 a9 f0 4f ec d5 87

Output T2:

29 f6 0d da 45 7b f2 19 aa 2e f9 5d 7a 59 be 95  
4d e0 08 f4 a5 0d 50 4d bd b6 90 be 68 06 01 53

## 7) PRF\_IPSEC\_KEYMAT\_GOSTR3411\_2012\_512

Key K:

c9 a9 a7 73 20 e2 cc 55 9e d7 2d ce 6f 47 e2 19  
2c ce a9 5f a6 48 67 05 82 c0 54 c0 ef 36 c2 21

Data of S:

01 26 bd b8 78 00 1d 80 60 3c 85 44 c7 27 01 00

Output T1:

b9 55 5b 29 91 75 4b 37 9d a6 8e 60 98 f5 b6 0e  
df 91 8a 56 20 4b ff f3 a8 37 6d 1f 57 ed b2 34  
a5 12 32 81 23 cd 6c 03 0b 54 14 2e 1e c7 78 2b  
03 00 be a5 7c c2 a1 4c a3 b4 f0 85 a4 5c d6 ca

Output T2:

37 b1 e0 86 52 43 a4 fb 29 14 8d 27 4d 30 63 fc  
bf b0 f2 f4 68 d5 27 e4 3b ca 41 fa 6b b5 3e c8  
df 21 bf c4 62 3a 2e 76 8b 64 54 03 3e 09 52 32  
d1 8c 86 a6 8f 00 98 d3 31 81 75 f6 59 05 ae db

8) PRF\_IPSEC\_ PRFPLUS\_GOSTR3411\_2012\_512

Key K:

c9 a9 a7 73 20 e2 cc 55 9e d7 2d ce 6f 47 e2 19  
2c ce a9 5f a6 48 67 05 82 c0 54 c0 ef 36 c2 21

Data of S:

01 26 bd b8 78 00 1d 80 60 3c 85 44 c7 27 01 00

Output T1:

5d a6 71 43 a5 f1 2a 6d 6e 47 42 59 6f 39 24 3f  
cc 61 57 45 91 5b 32 59 10 06 ff 78 a2 08 63 d5  
f8 8e 4a fc 17 fb be 70 b9 50 95 73 db 00 5e 96  
26 36 98 46 cb 86 19 99 71 6c 16 5d d0 6a 15 85

Output T2:

48 34 49 5a 43 74 6c b5 3f 0a ba 3b c4 6e bc f8  
77 3c a6 4a d3 43 c1 22 ee 2a 57 75 57 03 81 57  
ee 9c 38 8d 96 ef 71 d5 8b e5 c1 ef a1 af a9 5e  
be 83 e3 9d 00 e1 9a 5d 03 dc d6 0a 01 bc a8 e3

9) VKO\_GOSTR3410\_2012\_256 with 256-bit output on the GOST R  
34.10-2012 keys (512-bit output) with id-tc26-gost-  
3410-12-512-paramSetA

UKM value:

1d 80 60 3c 85 44 c7 27

Private key x of A:

c9 90 ec d9 72 fc e8 4e c4 db 02 27 78 f5 0f ca  
c7 26 f4 67 08 38 4b 8d 45 83 04 96 2d 71 47 f8  
c2 db 41 ce f2 2c 90 b1 02 f2 96 84 04 f9 b9 be  
6d 47 c7 96 92 d8 18 26 b3 2b 8d ac a4 3c b6 67

Public key  $x \cdot P$  of A (curve point (X, Y)):

aa b0 ed a4 ab ff 21 20 8d 18 79 9f b9 a8 55 66  
54 ba 78 30 70 eb a1 0c b9 ab b2 53 ec 56 dc f5  
d3 cc ba 61 92 e4 64 e6 e5 bc b6 de a1 37 79 2f  
24 31 f6 c8 97 eb 1b 3c 0c c1 43 27 b1 ad c0 a7  
91 46 13 a3 07 4e 36 3a ed b2 04 d3 8d 35 63 97  
1b d8 75 8e 87 8c 9d b1 14 03 72 1b 48 00 2d 38  
46 1f 92 47 2d 40 ea 92 f9 95 8c 0f fa 4c 93 75  
64 01 b9 7f 89 fd be 0b 5e 46 e4 a4 63 1c db 5a

Private key y of part B:

48 c8 59 f7 b6 f1 15 85 88 7c c0 5e c6 ef 13 90  
cf ea 73 9b 1a 18 c0 d4 66 22 93 ef 63 b7 9e 3b  
80 14 07 0b 44 91 85 90 b4 b9 96 ac fe a4 ed fb  
bb cc cc 8c 06 ed d8 bf 5b da 92 a5 13 92 d0 db

Public key  $y \cdot P$  of B (curve point (X, Y)):

19 2f e1 83 b9 71 3a 07 72 53 c7 2c 87 35 de 2e  
a4 2a 3d bc 66 ea 31 78 38 b6 5f a3 25 23 cd 5e  
fc a9 74 ed a7 c8 63 f4 95 4d 11 47 f1 f2 b2 5c  
39 5f ce 1c 12 91 75 e8 76 d1 32 e9 4e d5 a6 51  
04 88 3b 41 4c 9b 59 2e c4 dc 84 82 6f 07 d0 b6  
d9 00 6d da 17 6c e4 8c 39 1e 3f 97 d1 02 e0 3b  
b5 98 bf 13 2a 22 8a 45 f7 20 1a ba 08 fc 52 4a  
2d 77 e4 3a 36 2a b0 22 ad 40 28 f7 5b de 3b 79

KEK\_VKO value:

c9 a9 a7 73 20 e2 cc 55 9e d7 2d ce 6f 47 e2 19  
2c ce a9 5f a6 48 67 05 82 c0 54 c0 ef 36 c2 21

10) VKO\_GOSTR3410\_2012\_512 with 512-bit output on the GOST R  
34.10-2012 keys (512-bit output) with id-tc26-gost-

3410-12-512-paramSetA

UKM value:

1d 80 60 3c 85 44 c7 27

Private key x of A:

c9 90 ec d9 72 fc e8 4e c4 db 02 27 78 f5 0f ca  
c7 26 f4 67 08 38 4b 8d 45 83 04 96 2d 71 47 f8  
c2 db 41 ce f2 2c 90 b1 02 f2 96 84 04 f9 b9 be  
6d 47 c7 96 92 d8 18 26 b3 2b 8d ac a4 3c b6 67

Public key  $x \cdot P$  of A (curve point (X, Y)):

aa b0 ed a4 ab ff 21 20 8d 18 79 9f b9 a8 55 66  
54 ba 78 30 70 eb a1 0c b9 ab b2 53 ec 56 dc f5  
d3 cc ba 61 92 e4 64 e6 e5 bc b6 de a1 37 79 2f  
24 31 f6 c8 97 eb 1b 3c 0c c1 43 27 b1 ad c0 a7  
91 46 13 a3 07 4e 36 3a ed b2 04 d3 8d 35 63 97  
1b d8 75 8e 87 8c 9d b1 14 03 72 1b 48 00 2d 38  
46 1f 92 47 2d 40 ea 92 f9 95 8c 0f fa 4c 93 75  
64 01 b9 7f 89 fd be 0b 5e 46 e4 a4 63 1c db 5a

Private key y of B:

48 c8 59 f7 b6 f1 15 85 88 7c c0 5e c6 ef 13 90  
cf ea 73 9b 1a 18 c0 d4 66 22 93 ef 63 b7 9e 3b  
80 14 07 0b 44 91 85 90 b4 b9 96 ac fe a4 ed fb  
bb cc cc 8c 06 ed d8 bf 5b da 92 a5 13 92 d0 db

Public key  $y \cdot P$  of B (curve point (X, Y)):

19 2f e1 83 b9 71 3a 07 72 53 c7 2c 87 35 de 2e  
a4 2a 3d bc 66 ea 31 78 38 b6 5f a3 25 23 cd 5e  
fc a9 74 ed a7 c8 63 f4 95 4d 11 47 f1 f2 b2 5c  
39 5f ce 1c 12 91 75 e8 76 d1 32 e9 4e d5 a6 51  
04 88 3b 41 4c 9b 59 2e c4 dc 84 82 6f 07 d0 b6  
d9 00 6d da 17 6c e4 8c 39 1e 3f 97 d1 02 e0 3b  
b5 98 bf 13 2a 22 8a 45 f7 20 1a ba 08 fc 52 4a  
2d 77 e4 3a 36 2a b0 22 ad 40 28 f7 5b de 3b 79

KEK\_VKO value:

79 f0 02 a9 69 40 ce 7b de 32 59 a5 2e 01 52 97  
ad aa d8 45 97 a0 d2 05 b5 0e 3e 17 19 f9 7b fa  
7e e1 d2 66 1f a9 97 9a 5a a2 35 b5 58 a7 e6 d9  
f8 8f 98 2d d6 3f c3 5a 8e c0 dd 5e 24 2d 3b df

11) Key derivation function KDF\_GOSTR3411\_2012\_256:

K\_in key:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

Label:

26 bd b8 78

Seed:

af 21 43 41 45 65 63 78

KDF(K\_in, label, seed) value:

a1 aa 5f 7d e4 02 d7 b3 d3 23 f2 99 1c 8d 45 34  
01 31 37 01 0a 83 75 4f d0 af 6d 7c d4 92 2e d9

12) Key derivation function KDF\_TREE\_GOSTR3411\_2012\_256

Output size of L:

512

K<sub>in</sub> key:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

Label:

26 bd b8 78

Seed:

af 21 43 41 45 65 63 78

Value of K<sub>1</sub>:

22 b6 83 78 45 c6 be f6 5e a7 16 72 b2 65 83 10  
86 d3 c7 6a eb e6 da e9 1c ad 51 d8 3f 79 d1 6b

Value of K<sub>2</sub>:

07 4c 93 30 59 9d 7f 8d 71 2f ca 54 39 2f 4d dd  
e9 37 51 20 6b 35 84 c8 f4 3f 9e 6d c5 15 31 f9



13) Key wrap and unwrap with the szOID\_Gost28147\_89\_TC26\_Z\_ParamSet parameters

Key K:

00 01 02 03 04 05 06 07 08 09 0a 0b 0c 0d 0e 0f  
10 11 12 13 14 15 16 17 18 19 1a 1b 1c 1d 1e 1f

UKM value:

af 21 43 41 45 65 63 78

Label:

26 bd b8 78

KEK\_e(UKM) = KDF(K\_e, label, UKM):

a1 aa 5f 7d e4 02 d7 b3 d3 23 f2 99 1c 8d 45 34  
01 31 37 01 0a 83 75 4f d0 af 6d 7c d4 92 2e d9

CEK\_MAC:

38 d5 8a a3

CEK\_ENC:

b9 fb 92 42 95 0f 84 3f 0f bd 5b 9a 5e cf 9f 17  
f7 9e 6d 21 58 16 56 de 6d c5 85 dd 62 7a 44 0a

#### Authors' Addresses

Stanislav Smyshlyaev (editor)  
CRYPTO-PRO  
18, Sushevsky val  
Moscow 127018  
Russian Federation

Phone: +7 (495) 995-48-20  
Email: sv@cryptopro.ru

Evgeny Alekseev  
CRYPTO-PRO  
18, Sushevsky val  
Moscow 127018  
Russian Federation

Email: alekseev@cryptopro.ru

Igor Oshkin  
CRYPTO-PRO  
18, Sushevsky val  
Moscow 127018  
Russian Federation

Email: oshkin@cryptopro.ru

Vladimir Popov  
CRYPTO-PRO  
18, Sushevsky val  
Moscow 127018  
Russian Federation

Email: vpopov@cryptopro.ru

Serguei Leontiev  
CRYPTO-PRO  
18, Sushevsky val  
Moscow 127018  
Russian Federation

Phone: +7 (495) 933 11 68  
Email: vpopov@cryptopro.ru

Vladimir PodobaeV  
FACTOR-TS  
11A, 1st Magistralny proezd  
Moscow 123290  
Russian Federation

Phone: +7 (495) 644-31-30  
Email: v\_podobaev@factor-ts.ru

Dmitry Belyavsky  
TCI  
8, Zoologicheskaya st  
Moscow 117218  
Russian Federation

Phone: +7 (499) 254-24-50  
Email: beldmit@gmail.com